

# Opening the design space by removing constraints with Additive Manufacturing and Topology Optimization

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# The Micro and Nanoscale Design (MnD) Group

- NTNU- Department of Mechanical and Industrial Engineering
- 6 PhD/ 6 Master Students
- Publications (2017-2020): 44 Journal Articles/ 1 Patent
- 1 Frinatek grant (similar to FWF Start), 1 ERC grant
- Supported by Stanford University and TU Wien



# New possibilities through AM



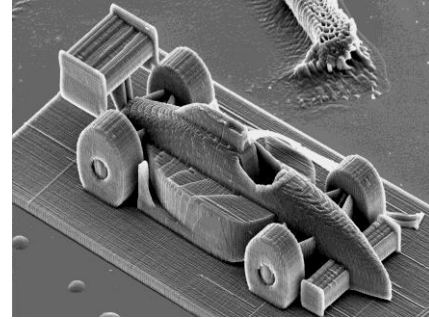
mx3D.com



ems-usa.com/



Stratasys.com



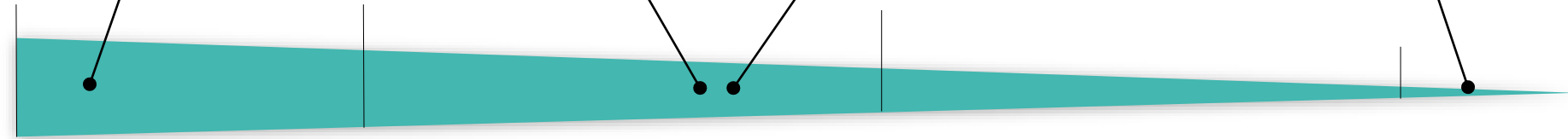
TU Wien 2012

100 m

1 m

1 mm

1  $\mu\text{m}$  100 nm

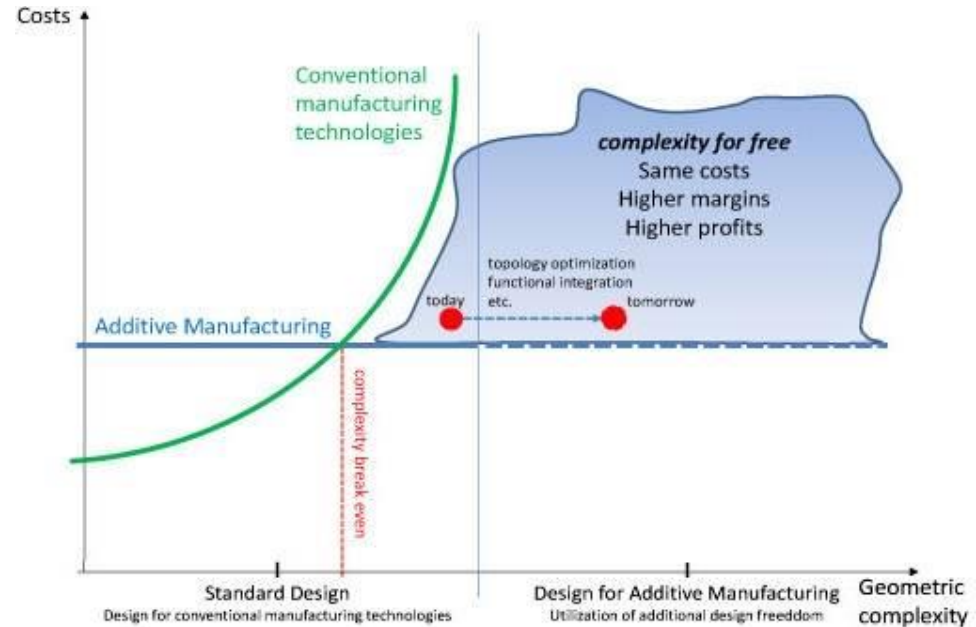
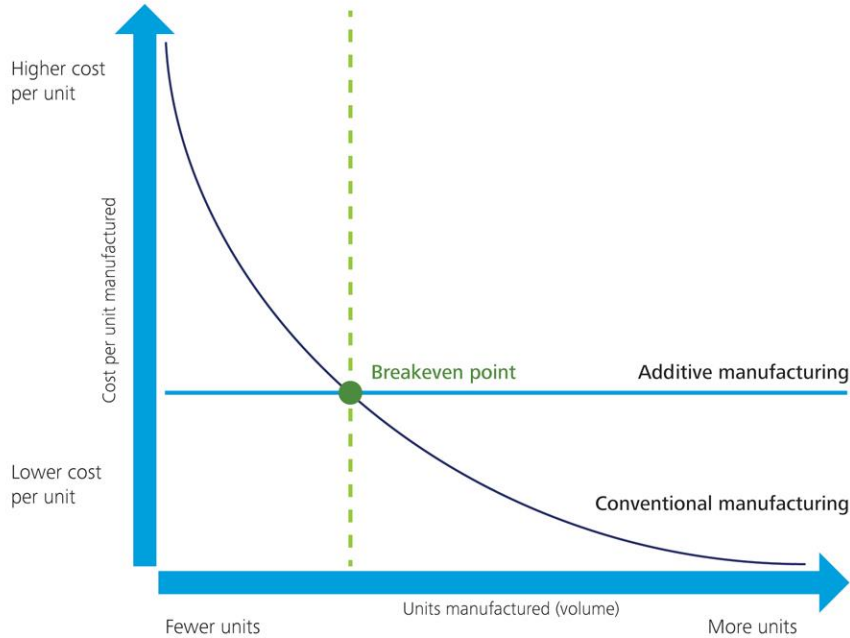


# New possibilities through AM



<https://www.youtube.com/watch?v=GUdnrtjT5Q>

# Possibilities in design through additive production



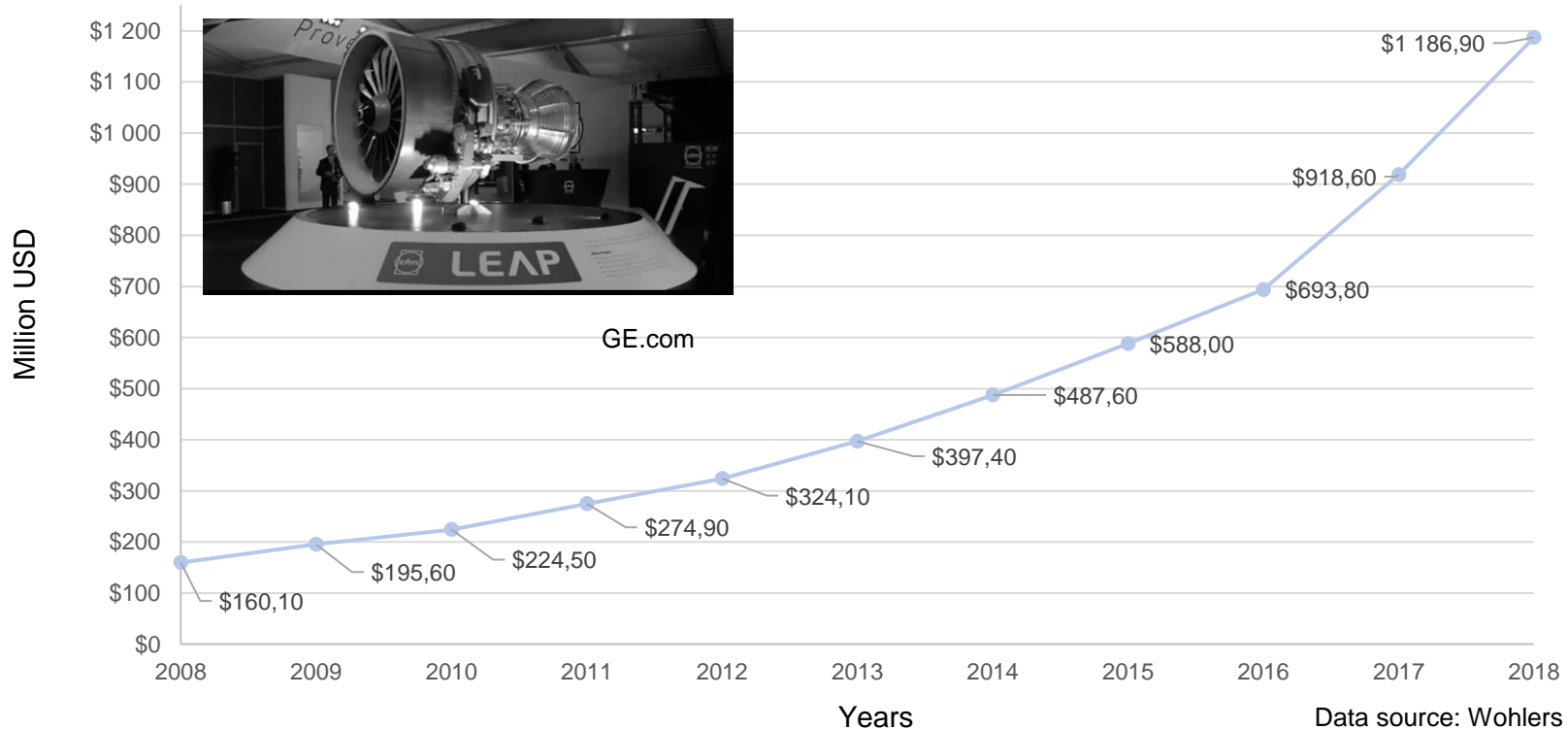
Source: Mark Cotteleer and Jim Joyce, *3D opportunity: Additive manufacturing paths to performance, innovation, and growth*, Deloitte University Press, <http://dupress.com/articles/dr14-3d-opportunity/>, accessed March 17, 2015.

Graphic: Deloitte University Press | DUPress.com

Farina.com

# Possibilities in design through additive production

Revenue From Final Part Production



Data source: Wohlers Associates, Inc.

# AM and Data Driven Design

## Additive Manufacturing

- No tools
- Minimal material waste
- Low manufacturing constraints
- Production time dependent on material used



## Data Driven Design

- Less design restrictions lead to an extended solution space
- Among more solutions there is always a «better» one

# Design to...

Additive Manufacturing

Data Driven Design



Save Material

Gain performance

Reuse



# Design to...

**Additive Manufacturing**

**Data Driven Design**

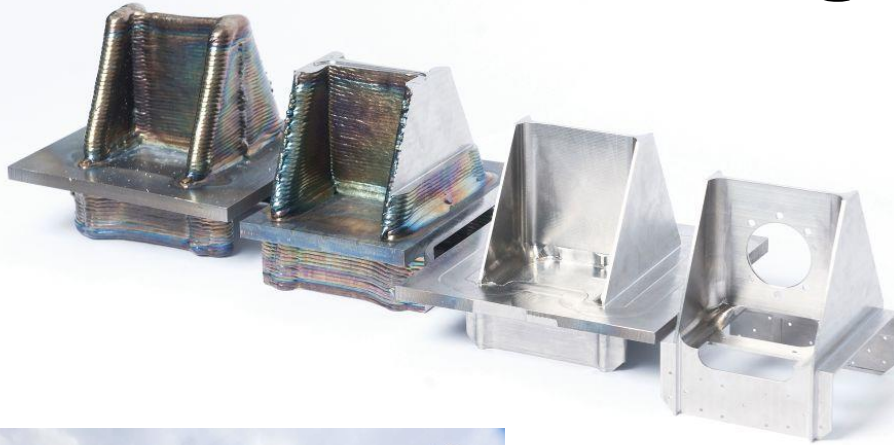


**Save Material**

**Reuse**

**Gain performance**

# Materials Saving- Near Net Shape



Norsk Titanium Høynefoss

[norsktitanium.com](http://norsktitanium.com)

# Materials Saving- Near Net Shape

Part build size: 900mm x 600mm x 300mm

Layer dimensions: H = 3–4 mm; W = 8–12 mm

Deposition rate: 5–10 kg/hour

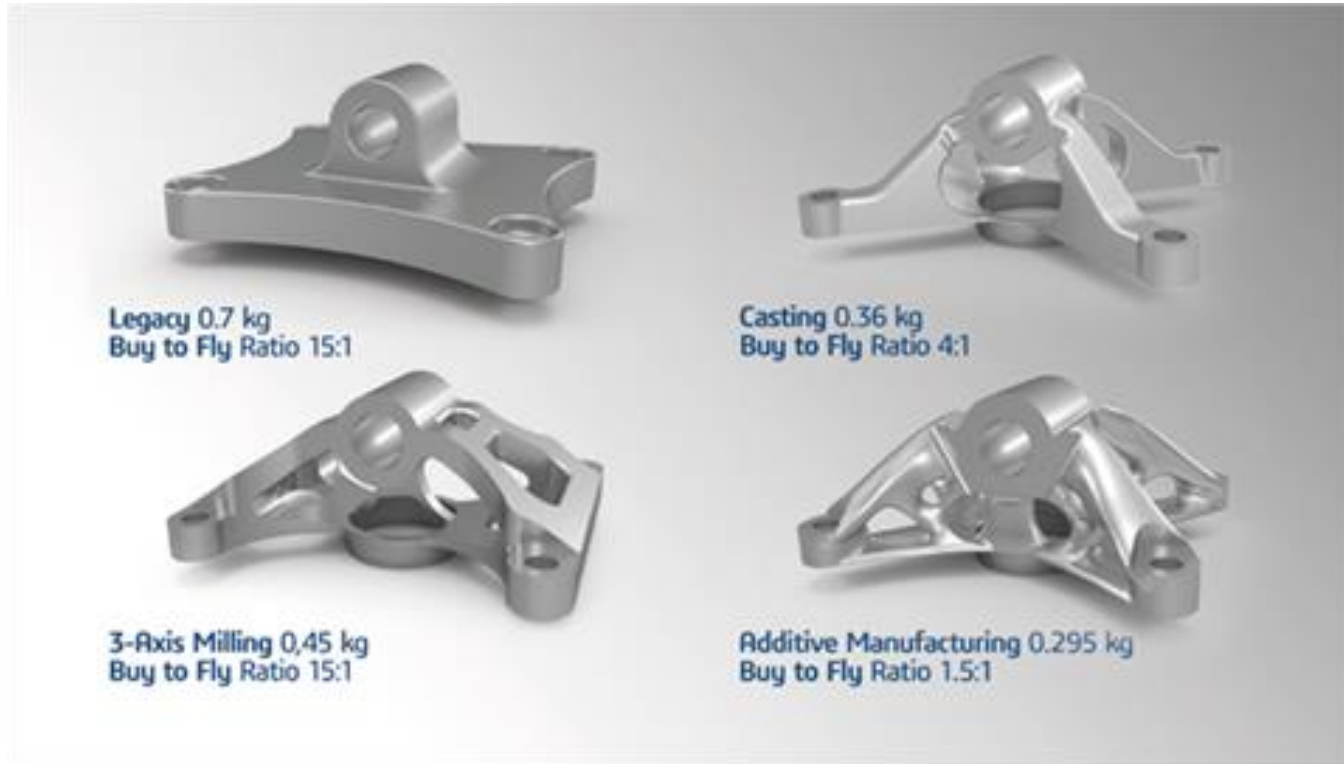
Titanium, Nickel Alloys, Tool Steel, Stainless Steel

High Volume Production: 10-20 metric tons annually



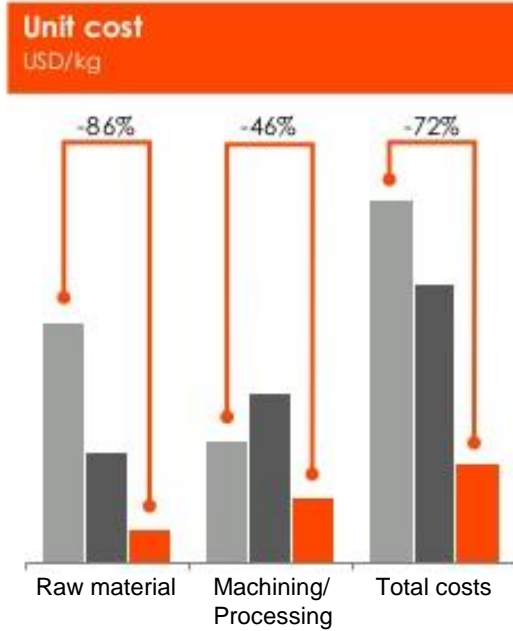
<http://www.norsktitanium.com/>

# Materials Saving- Near Net Shape



3ds.com

# Materials Saving- Near Net Shape



	Forged block Quoted	Die forging Quoted	DMD Estimated
Raw material cost (USD/kg)	~55	~88	~65*
Buy-to-fly ratio	16:1	6:1	1.5:1
Weight (kg)	~210	~82	~20



» **Specifications for sample unit used for comparison:**

- Component produced in low volume (40 components/year)
- Dimensions: 406 x 508 x 229 mm
- **Finished product weight: ~13 kg**

\* Assumed cost for wire

Slide 22

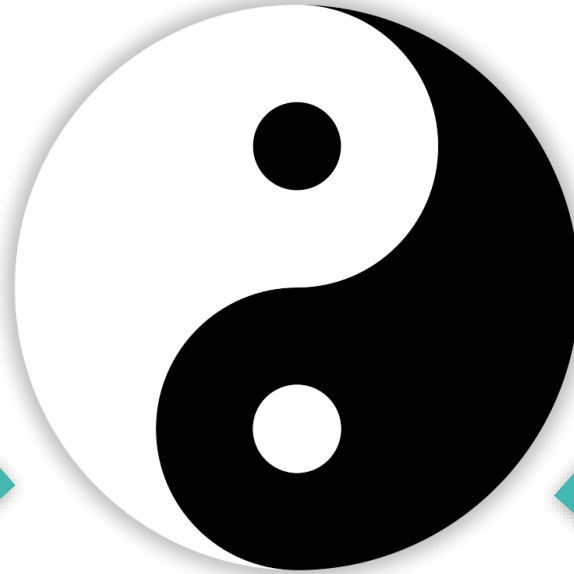


Courtesy of Norsk Titanium

# Design to...

Additive Manufacturing

Topology Optimization



Save Material

Reuse

Gain performance

# High Stiffness/ Low Weight



<20k \$/kg



<1k \$/kg



<100 \$/kg



<5 \$/kg

# High Stiffness/ Low Weight

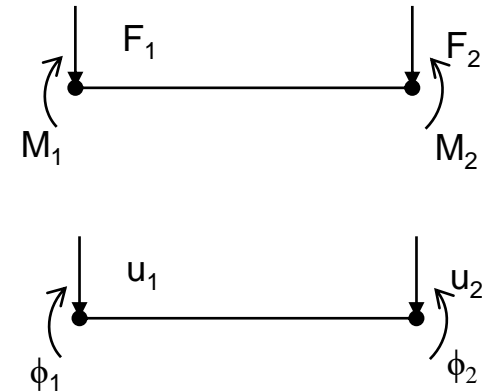
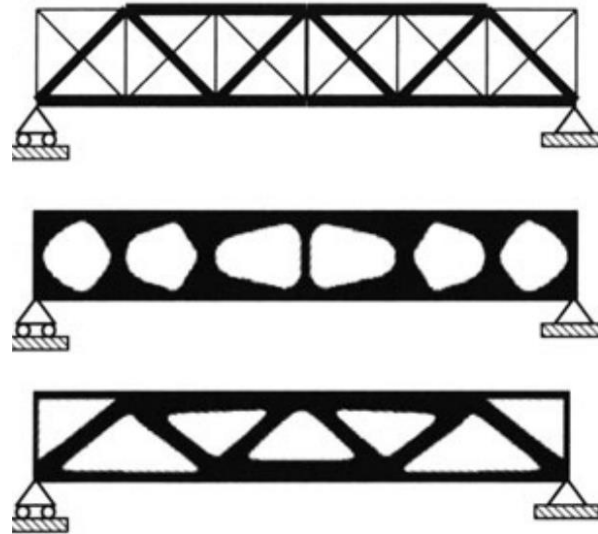


Courtesy of Jürgen Stampfl, TU Wien



# Structural Optimization- Overview

- The Design Domain
- Objective Function
- Boundary Conditions
- Homogenization of Stress Level
- Minimum Compliance



# What is Topology Optimization?

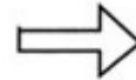
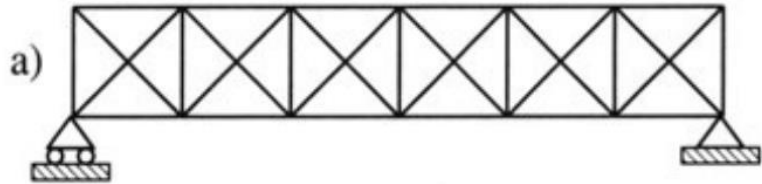
Design variable

State variable

Thickness

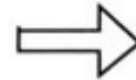
Deflection

Sizing



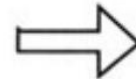
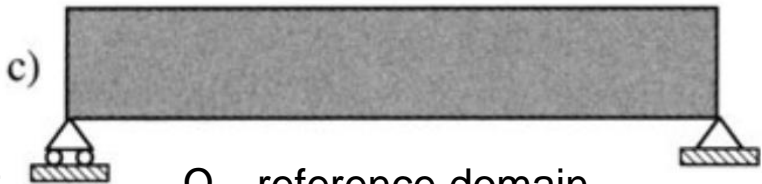
Shape-  
Optimization

Domain



Topology-  
Optimization

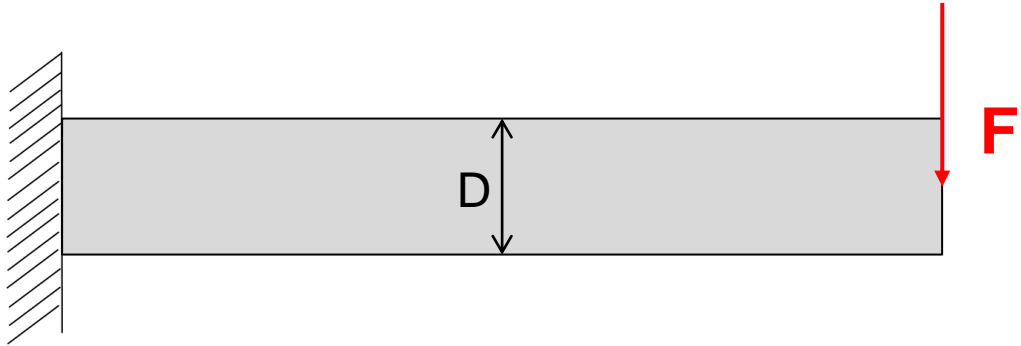
$\Omega$ ...reference domain



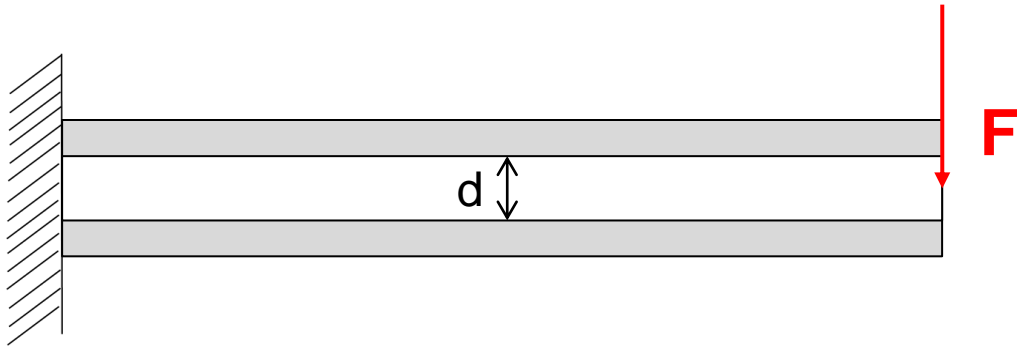
$\Omega^{\text{mat}}$ ...part domain

# What is Topology Optimization?

Sizing

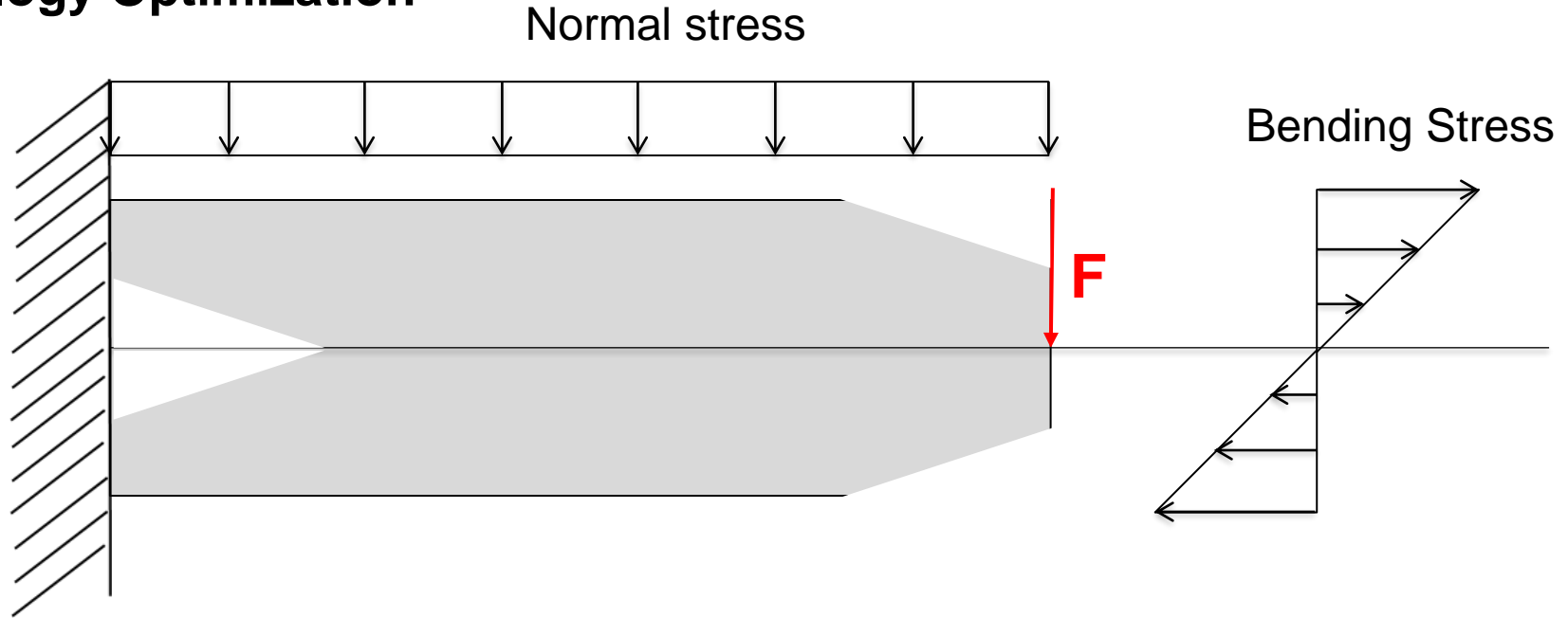


Shaping



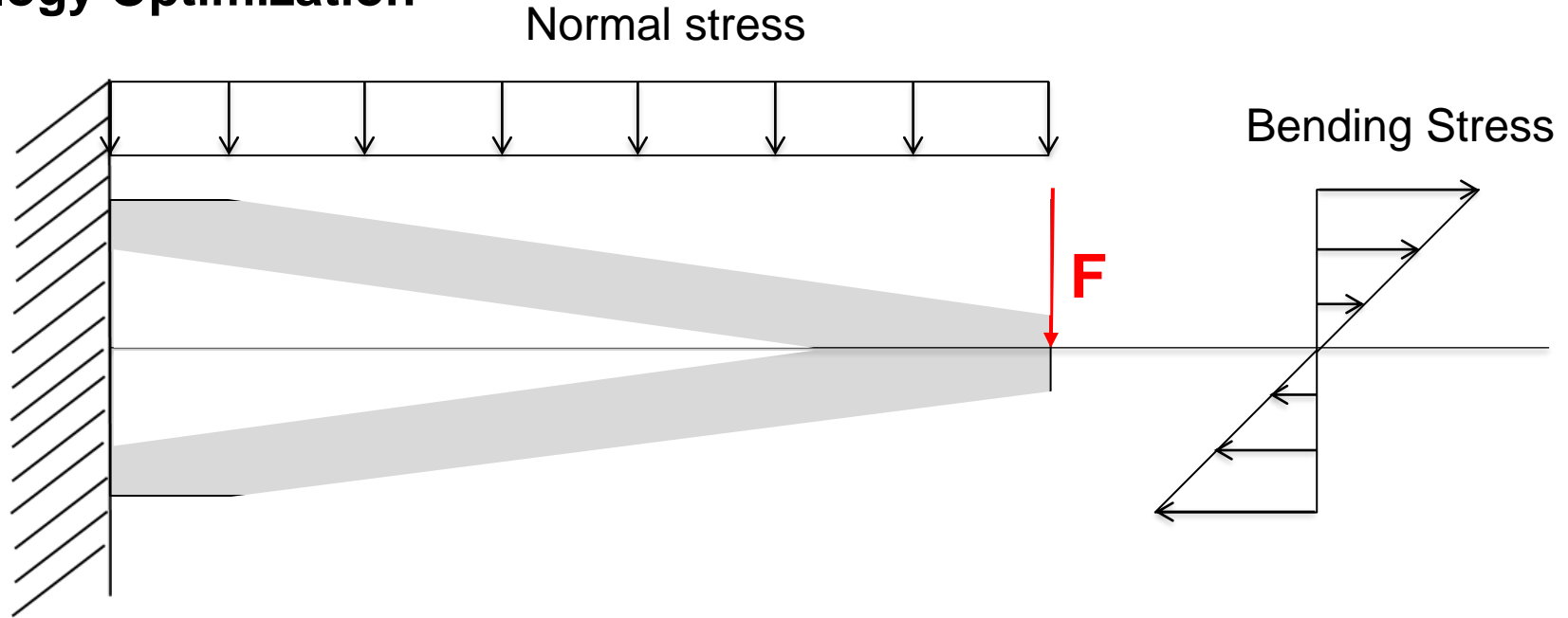
# What is Topology Optimization?

## Topology Optimization



# What is Topology Optimization?

## Topology Optimization



# Stress-strain relationship and stiffness matrix for isotropic material

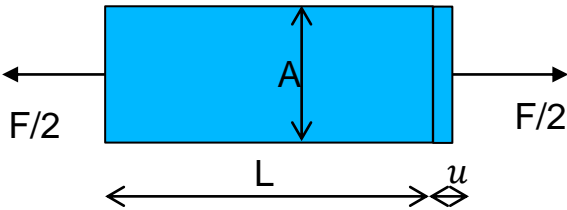
Hooke's law

$$\sigma = \frac{F}{A}$$

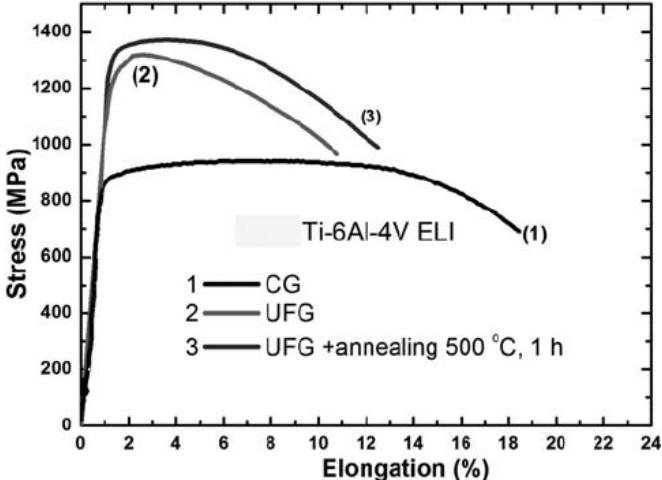
$$\epsilon = \frac{\delta}{L}$$

$$\epsilon = \frac{\sigma}{E} = \frac{F}{AE}$$

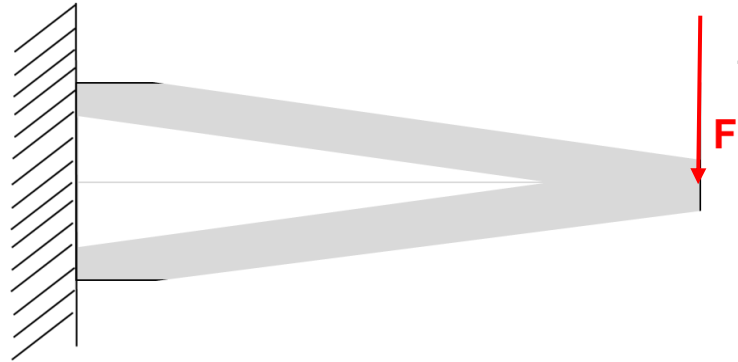
$$u = \epsilon L = \frac{FL}{AE}$$



$\sigma$ ...Normal stress  
 $F$ ...Applied load  
 $\epsilon$ ...Normal strain  
 $\delta$ ...Change in length  
 $L$ ...Original length  
 $E$ ...Elastic modulus



# What is Stiffness?



F and I are defined by product function and can therefore usually not be changed

$$\delta_{max} = \frac{Fl^3}{3EI}$$

Stiffer Material?

E/ρ?

Steel: 25.5

Ti: 25.5

Al: 26

[10<sup>6</sup> m<sup>2</sup>/s<sup>2</sup>]

Steel:

10x10

650xl

Aluminium:

16.5x16.5

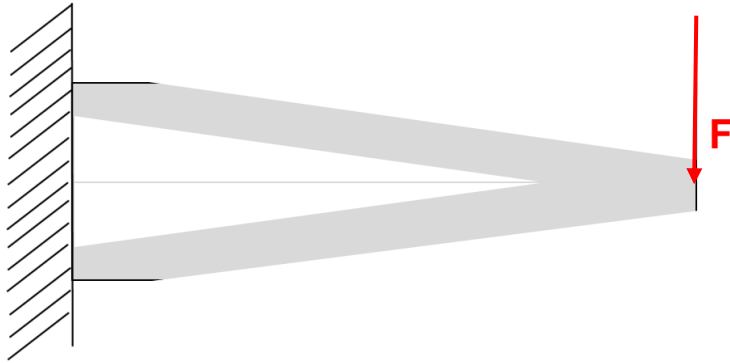
# What is Stiffness?

F and I is defined by product function and can therefore usually not be changed

$$\delta_{max} = \frac{Fl^3}{3EI}$$

More utilization of design domain?

Stiffer Material?



Hollow structure:

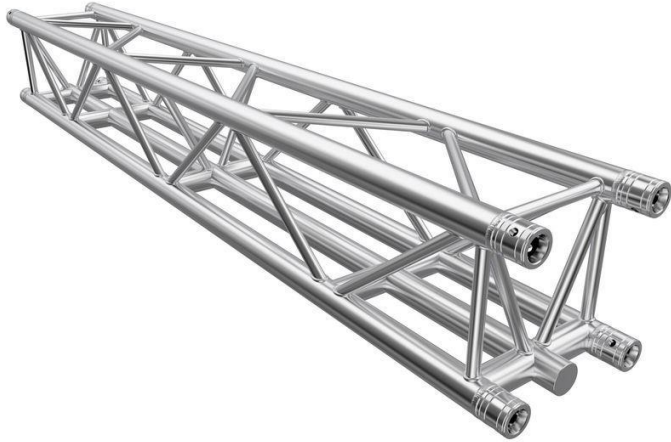
14x14

2400x1

50x50x1



# What is Stiffness?



Truss: High directional stiffness  
geometrically simple



Shell: High global stiffness, high  
eigenfrequencies

# What is Stiffness?

## Key Takeaways

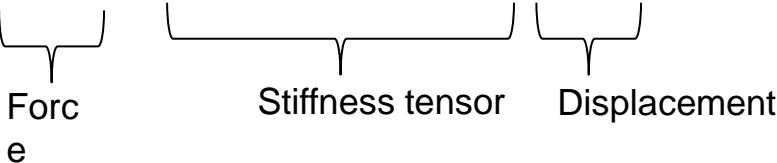
- Use the largest design domain possible
- Use a low density material to maximize I
- Optimization of material cross section important

# Stress-strain relationship and stiffness matrix for isotropic material

Tensor Form

$$f_s = ku$$

$$\begin{bmatrix} F_1 \\ M_1 \\ F_2 \\ M_2 \end{bmatrix} = \begin{bmatrix} k_{11} & k_{12} & k_{13} & k_{14} \\ k_{21} & k_{22} & k_{23} & k_{24} \\ k_{31} & k_{32} & k_{33} & k_{34} \\ k_{41} & k_{42} & k_{43} & k_{44} \end{bmatrix} \begin{bmatrix} u_1 \\ \phi_1 \\ u_2 \\ \phi_2 \end{bmatrix}$$

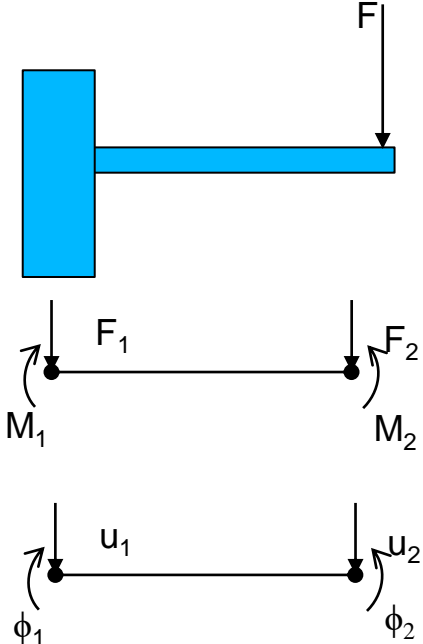


Equivalent Stress- Von Mises

Stress

$$\sigma_{vm} = \sqrt{\sigma_1^2 - \sigma_1\sigma_2 + \sigma_2^2}$$

f...Load vector  
 u...Displacement vector  
 k...Stiffness tensor



# Stress homogenization based Structural Optimization

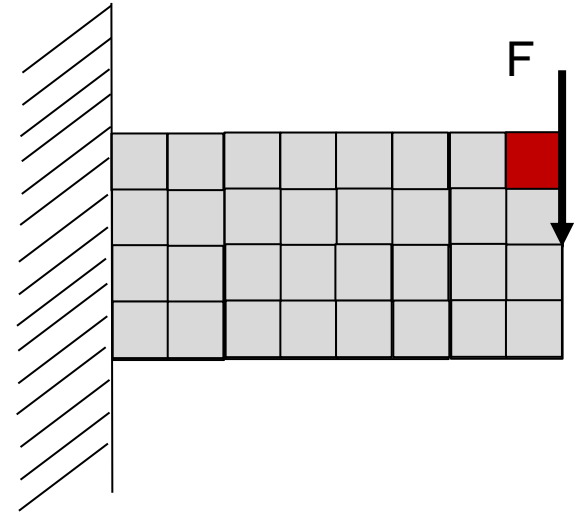
Objective Function  
Boundary Conditions

(1) 
$$\overset{\text{Volume}}{V} = \sum_{i=1}^N \overset{\text{Relative density}}{x_i} * \overset{\text{Volume of element}}{v_i}$$

Elements in the design domain

(2) 
$$\frac{\overset{\text{Von mises stress}}{\sigma_e^{vm}}}{\overset{\text{Yield strength}}{\sigma_{yield}}} < R R i \text{ --- Current rejection ratio}$$

(3) 
$$\overset{\text{Global stiffness matrix}}{KU} = \overset{\text{Global force}}{F} \text{ --- Global displacement vector}$$



(4) 
$$x_i \begin{cases} 1 \in \Omega_{mat}/\Omega \\ 0 \notin \Omega_{mat}/\Omega \end{cases}$$

# Stress homogenization based Structural Optimization

## Michell Type Structure

*“a frame (today called truss) (is optimal) attains the limit of economy of material possible in any frame-structure under the same applied forces, if the space occupied by it can be subjected to an appropriate small deformation, such that the strains in all the bars of the frame are increased by equal fractions of their lengths, not less than the fractional change of length of any element of the space.” (Michell 1904)*

Maxwell load-path theorem

Tension value in any tension element of length  $l_p$

$$\sum l_p f_p - \sum l_q f_q = C$$

Constant based on external loads/ supports

Compression value in any compression element of length  $l_q$

# Stress homogenization based Structural Optimization

## Gradually removing inefficient material from the structure

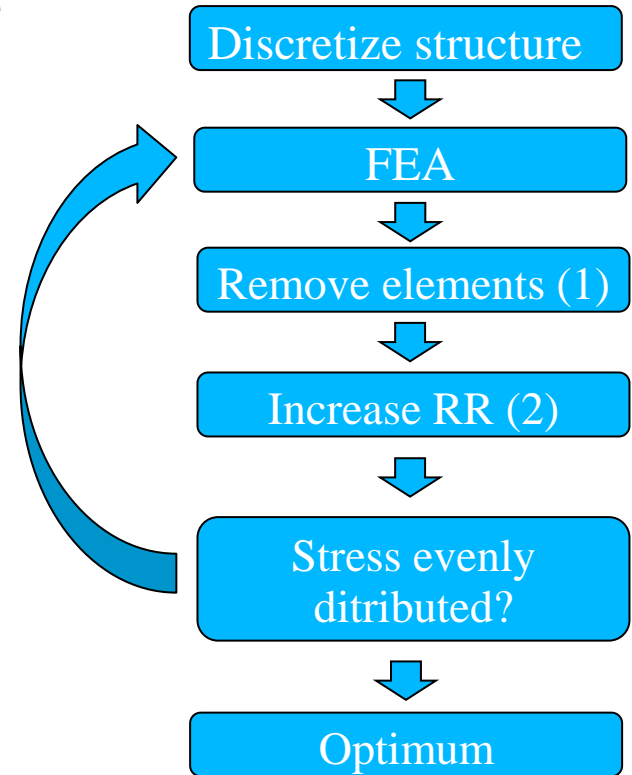
- Inefficiencies- low values of stress/strain
- Black and white rendering
- Reference domain  $\Omega$  in  $R^2$

$$(1) \quad \frac{\sigma_e^{vm}}{\sigma_{max}^{vm}} \leq RR_i$$

Von Mises stress of element  
Current rejection ratio  
Maximum van Mises stress of whole structure

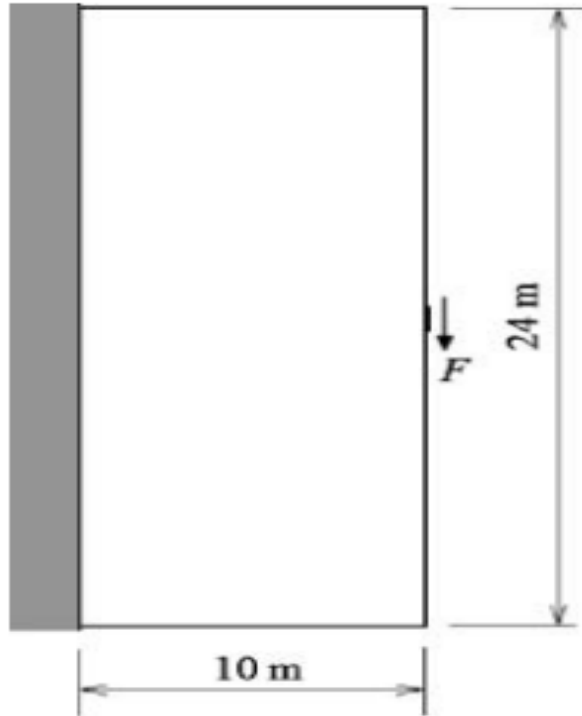
$$(2) \quad RR_{i+1} = RR_i + ER$$

Evolutionary rate

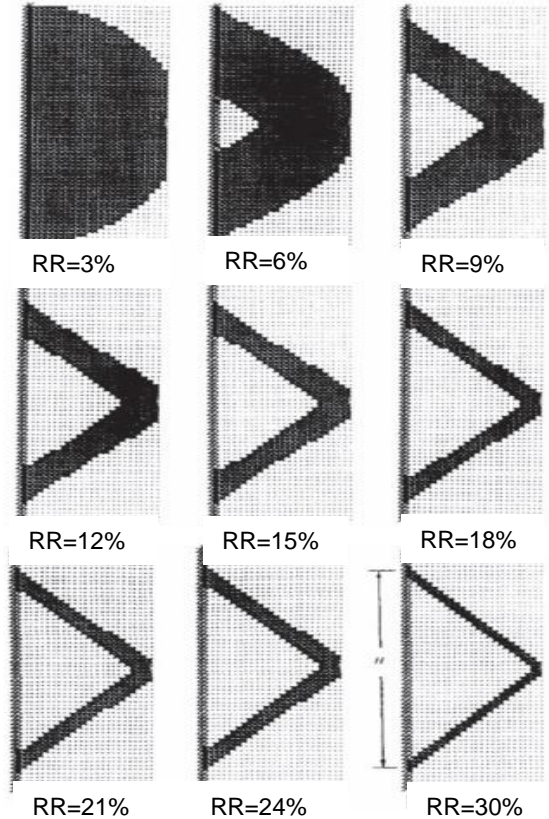


# Stress homogenization based Structural Optimization

## Michell Type Structure

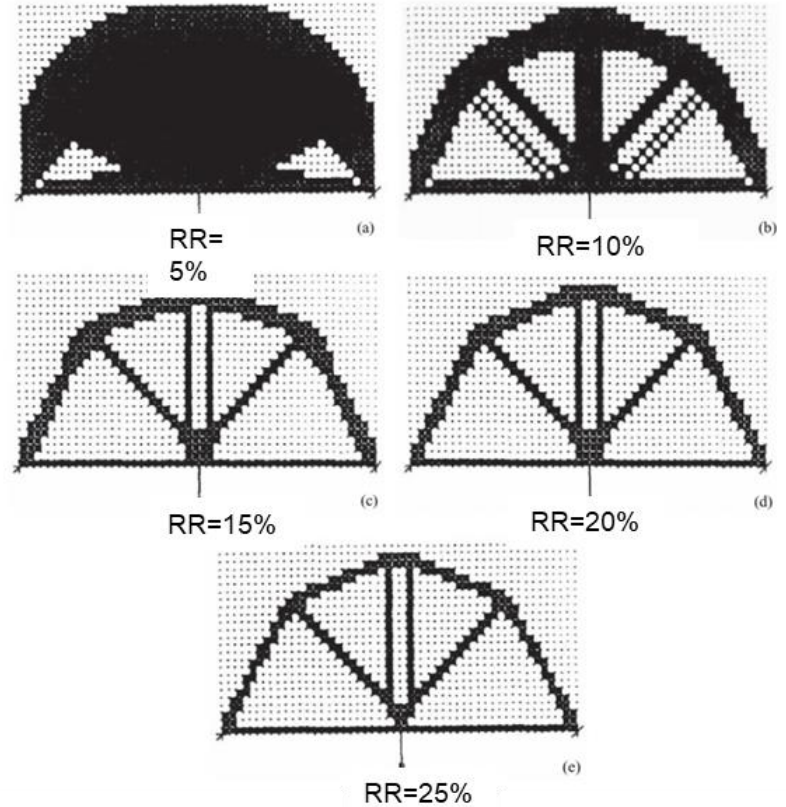
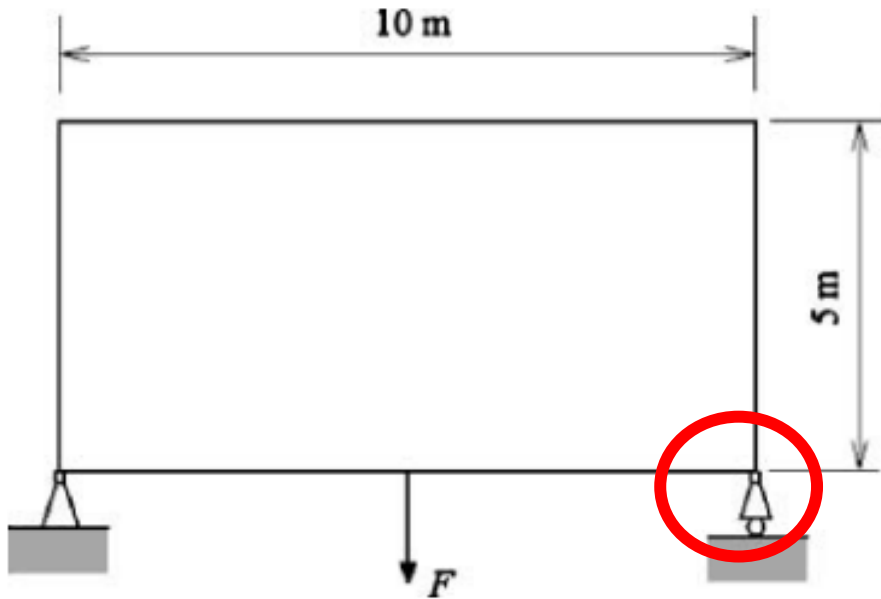


Steady state rejection ratios



# Stress homogenization based Structural Optimization

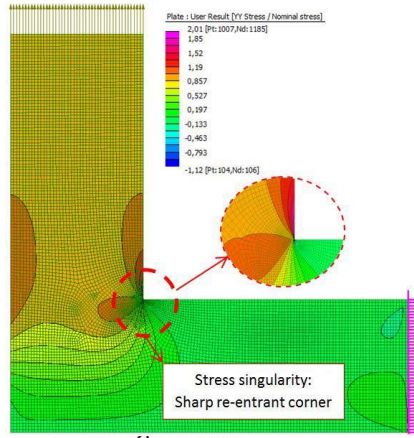
## Support Condition





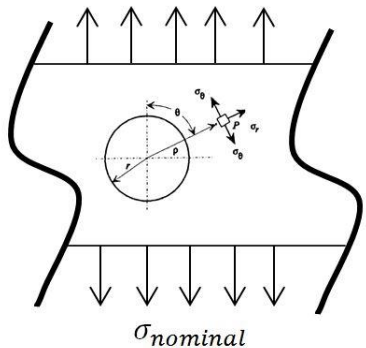
# Stress homogenization based Structural Optimization

Stress Singularities

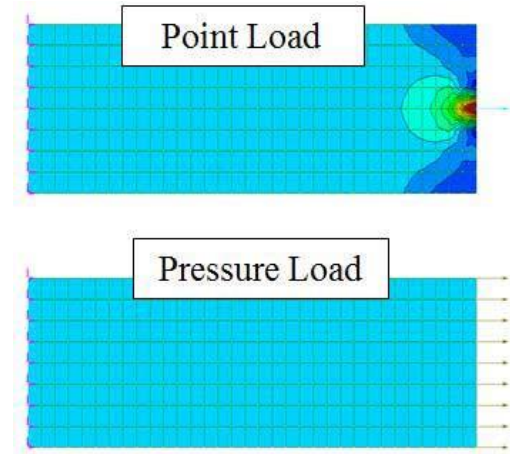


$\sigma_{nominal}$

Stress Concentrators



$\sigma_{nominal}$



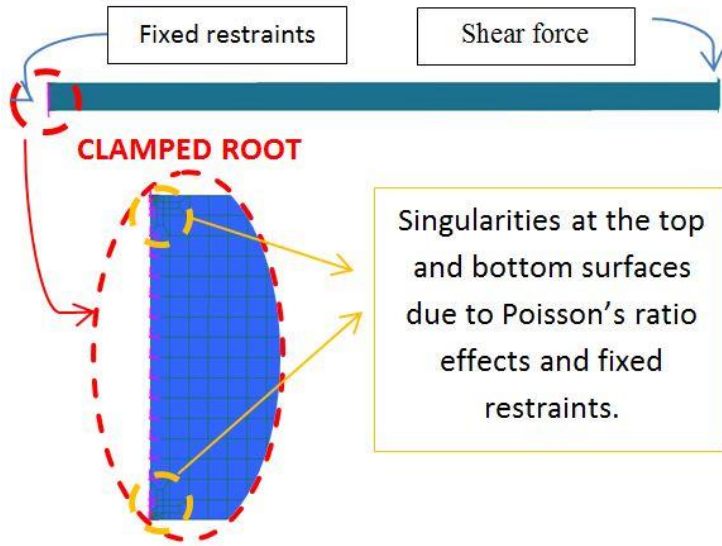
- Point load
- Sharp re-entrant corners
- Corners of bodies
- Point restraints

- Manufacturing produces fillet radiuses
- Finite stress value
- Hole in plate mesh, fillet corners, change of cross section,...

$$K_t = \frac{\sigma_{max}}{\sigma_{nom}} = 3$$

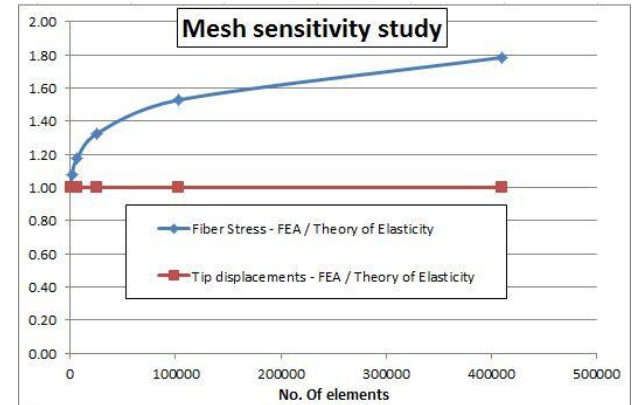
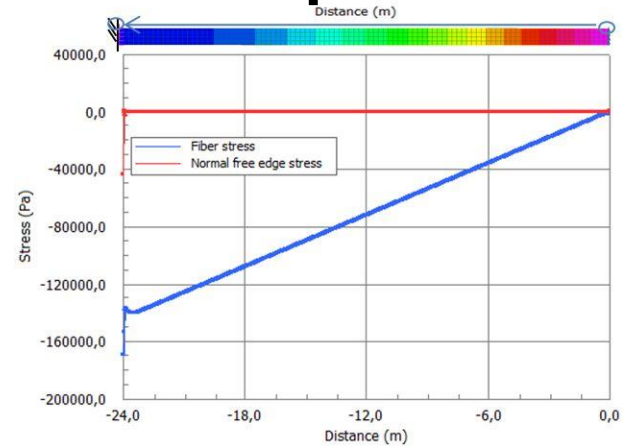
# Stress homogenization based Structural Optimization

- Stress singularities do not affect displacement results
- Occur at supports when displacement and stress conditions are mixed



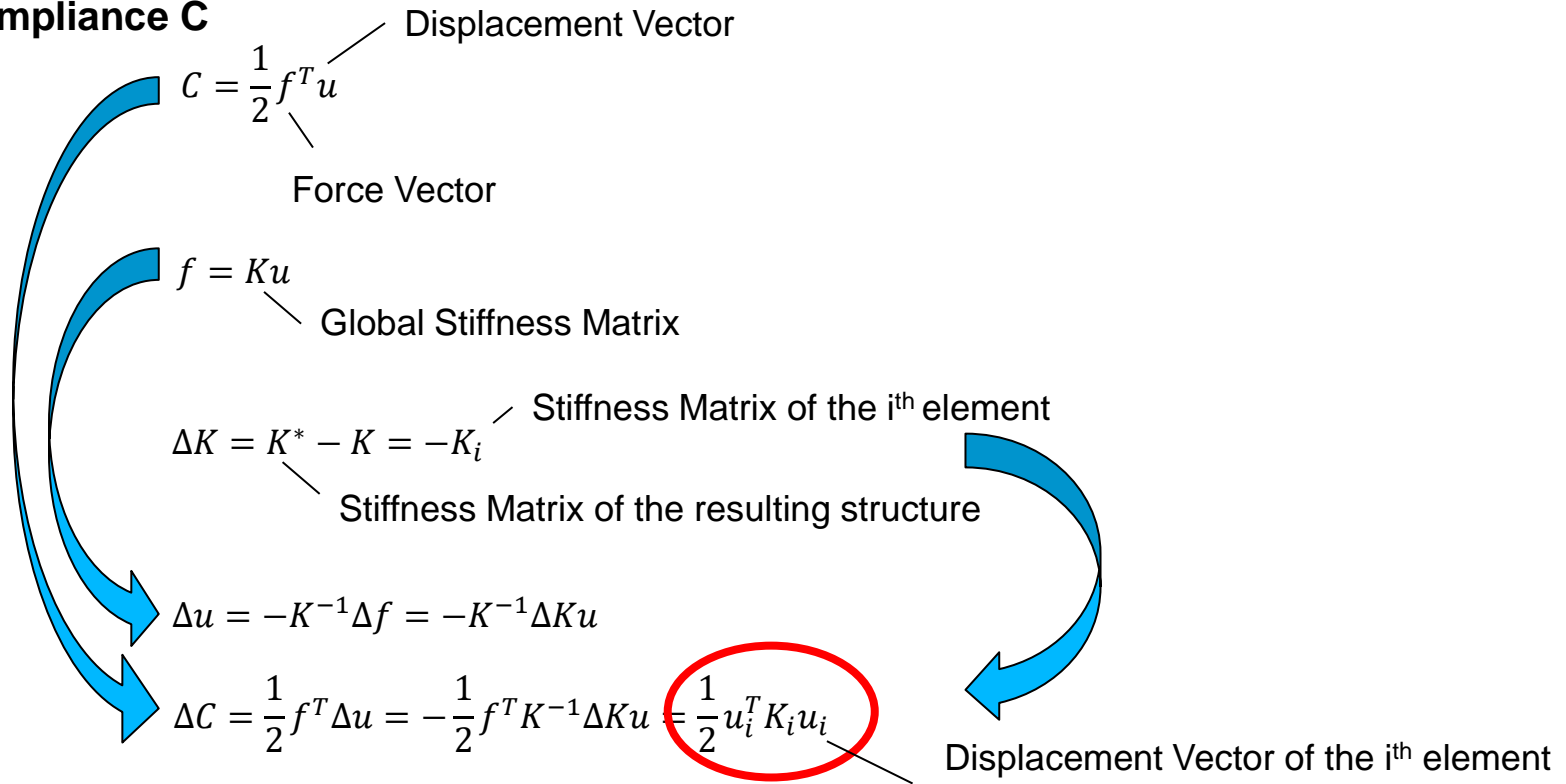
Singularities at the top and bottom surfaces due to Poisson's ratio effects and fixed restraints.

Shimels et al- IOP Conf. Ser.: Mater. Sci. Eng. 2017



# The Minimum Compliance Model

Mean Compliance  $C$



# The Minimum Compliance Model

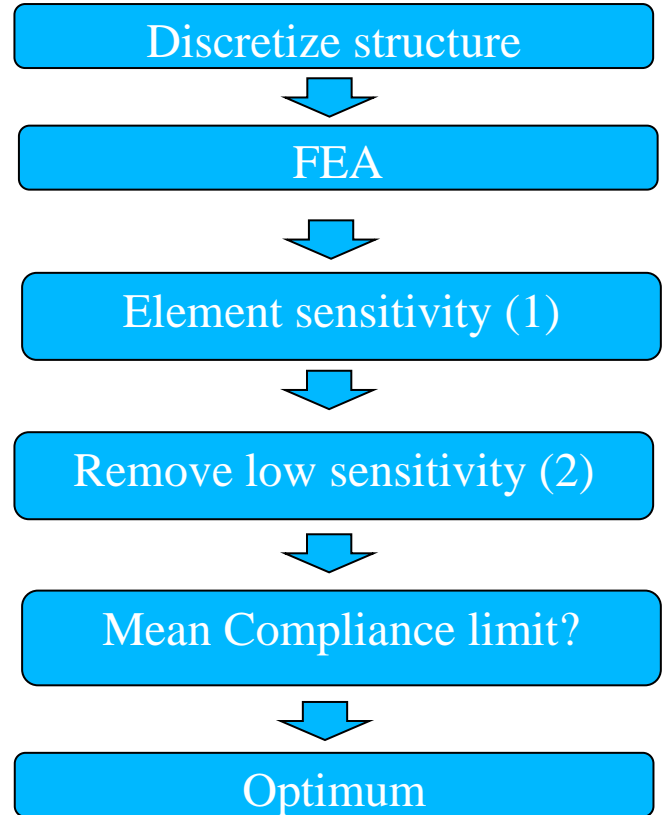
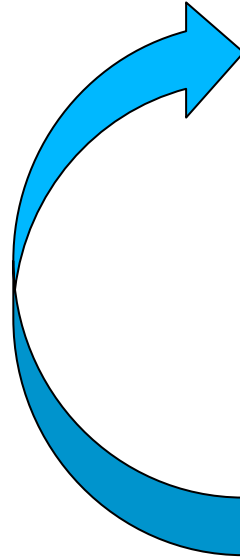
Mean Compliance C- Sensitivity number

$$\alpha_i^e = \frac{1}{2} u_i^T K_i u_i \quad (1)$$

Elemental removal ratio

$$ERR = \frac{\#elements\ removed}{\#total\ elements} \quad (2)$$

No steady state!



# The Minimum Compliance Model

Boundary Conditions Objective Function

Number of elements  $N$       Relative density

(1)  $C(x) = \sum_{i=1}^N x_i * u_i^T k_i u_i$

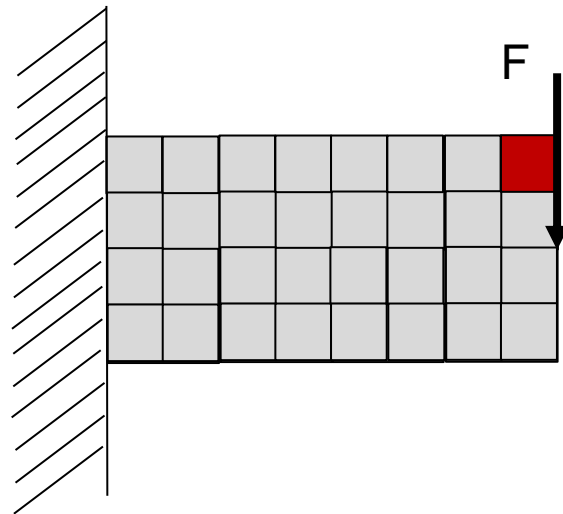
Elemental stiffness matrix  $k_i$   
 Elemental displacement  $u_i$   
 Elements in the design domain

(2)  $\frac{\Omega^{mat}}{\Omega} < \text{volfrac}$

Material domain volume  $\Omega^{mat}$   
 Design domain volume  $\Omega$   
 Desired volume  $\text{volfrac}$

(3)  $KU = F$

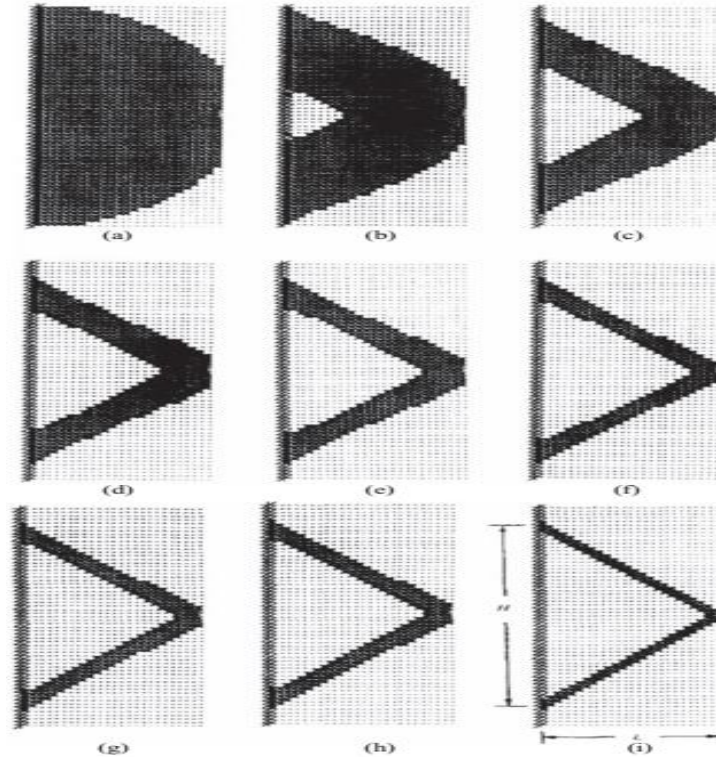
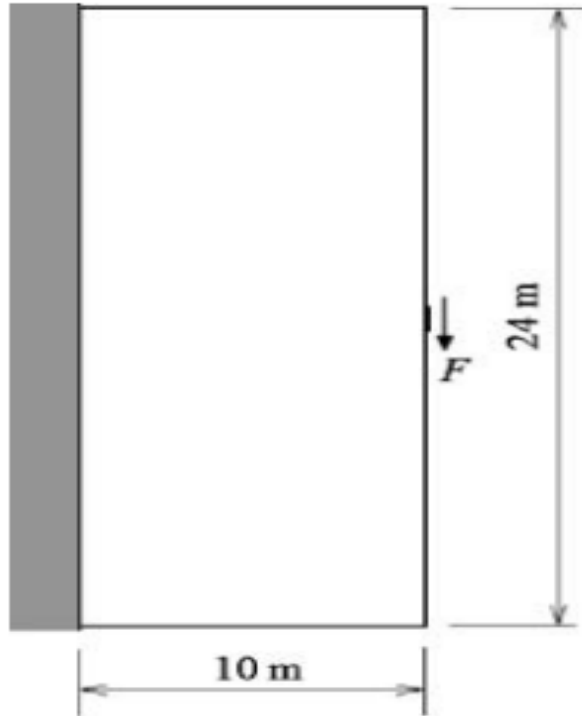
Global stiffness matrix  $K$   
 Global force  $F$   
 Global displacement vector  $U$



(4)  $x_i \begin{cases} 1 \in \Omega_{mat}/\Omega \\ 0 \notin \Omega_{mat}/\Omega \end{cases}$

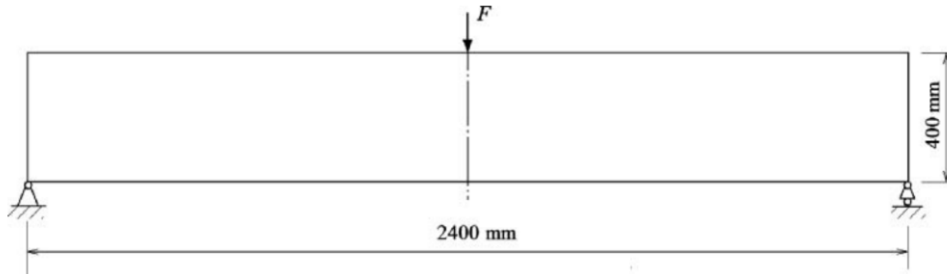
# The Minimum Compliance Model

Example: Short Cantilever



# The Minimum Compliance Model

## Example: Beam structure



- Half of structure modelled (symmetry)
- 60x20 four node (hexahedral) elements



ERR=1%; V=50%



ERR=2%; V=52%



ERR=4%; V=54%

# Minimum Compliance vs. Stress Homogenization

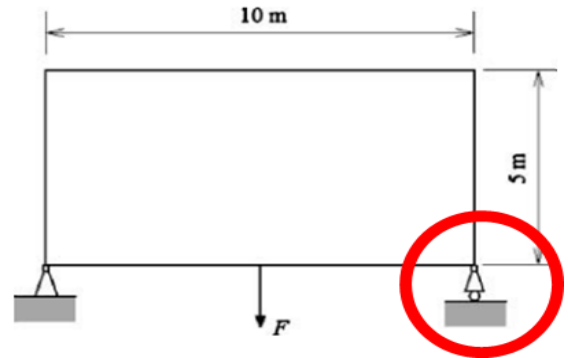
Stress level



Compliance based

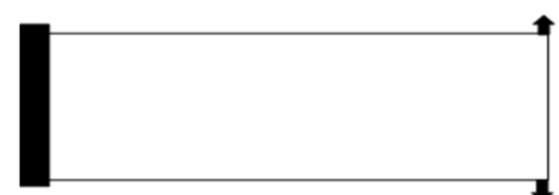
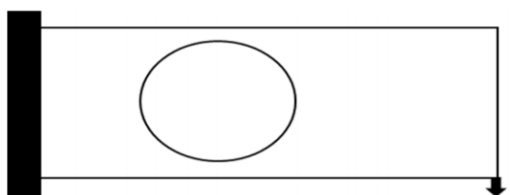
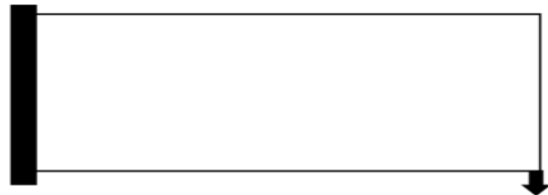


120 x 48 elements  
 $E = 1 \text{ Mpa}$   
 $\text{Volfrac} = 0,3$



Shimels et al- IOP Conf. Ser.: Mater. Sci. Eng. 2017

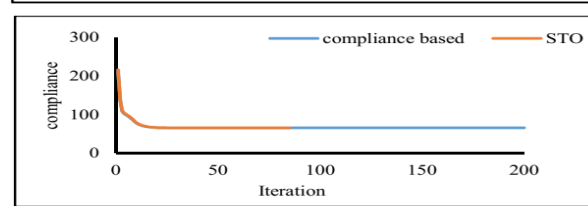
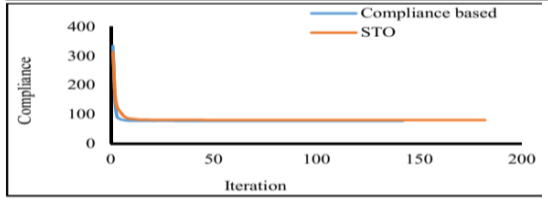
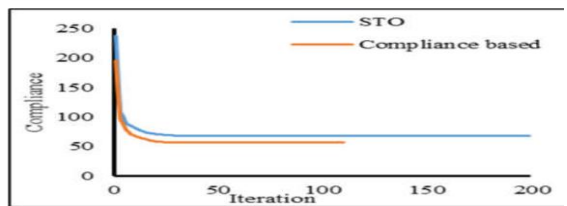
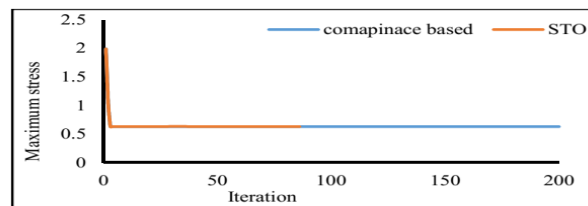
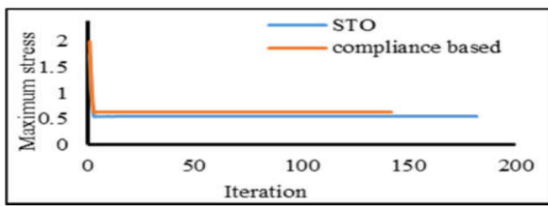
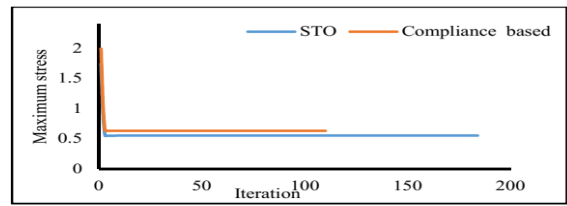




(a)

(b)

(c)



# Minimum Compliance vs. Stress Homogenization

## Stress level

- Material distributed to sustain loads
- Subject to defined boundary and load conditions
- Simpler structures
- Higher computational efforts
- Layout favors failure criterion and not material to be distributed
- More realistic
- Definition of stress constraint at element level difficult (singularity, local nature, nonlinear behavior)
- Less popular

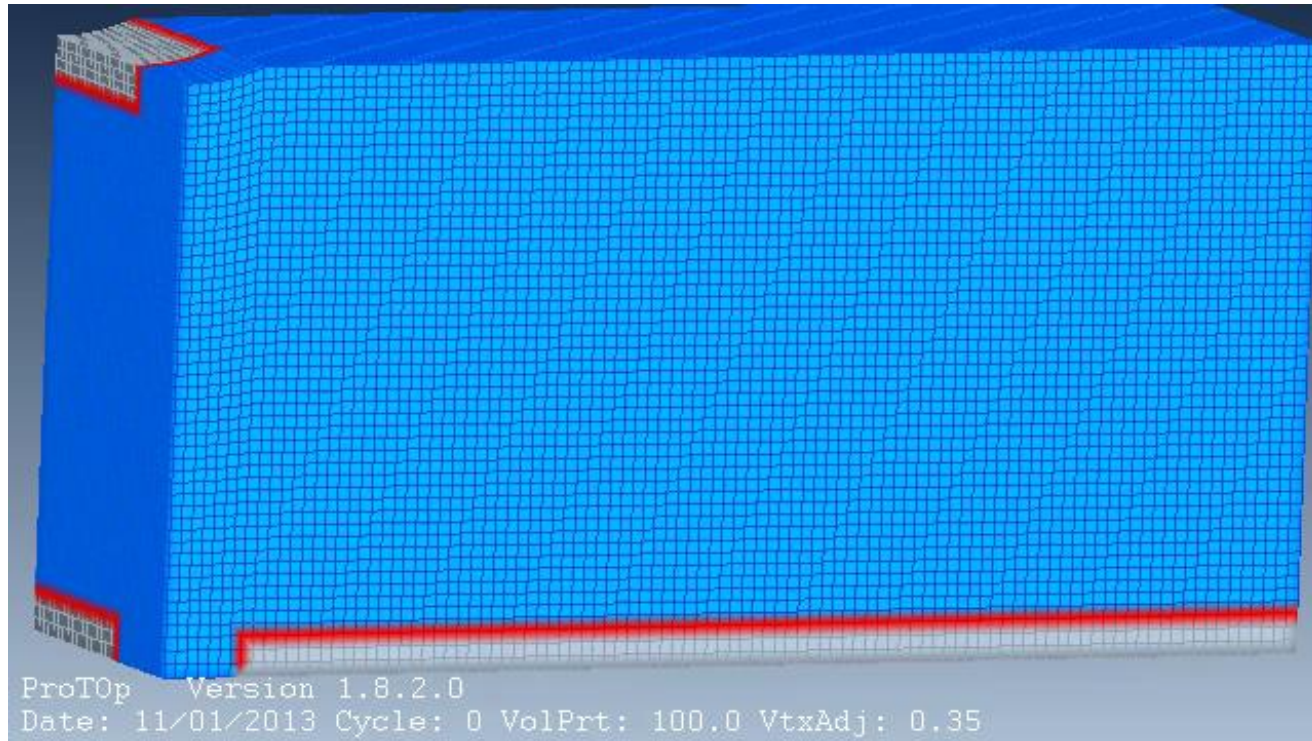
## Compliance minimization

- Optimal volume fraction boundary condition
- Optimal material distributions and induced stress are result of volume fraction
- Complex layout
- Dependent on the amount of material to be distributed
- Not exact in predicting stress and displacements
- Robust
- Lower computational effort
- Most common

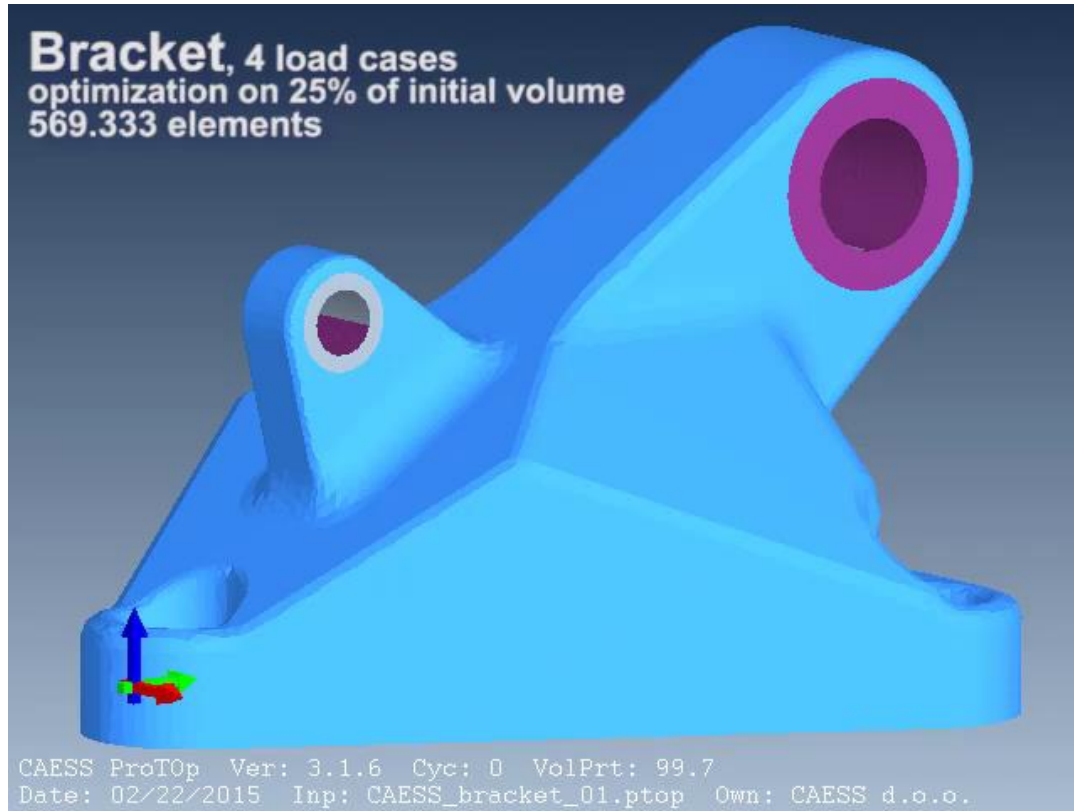
# The Minimum Compliance Model



# The Minimum Compliance Model



# The Minimum Compliance Model



# Compliance Model- An example

General requirements:

- Stiffness
- Weight
- Multi-purpose use

Housing:

- Wheel bearings
- Planetary gearbox

Connecting:

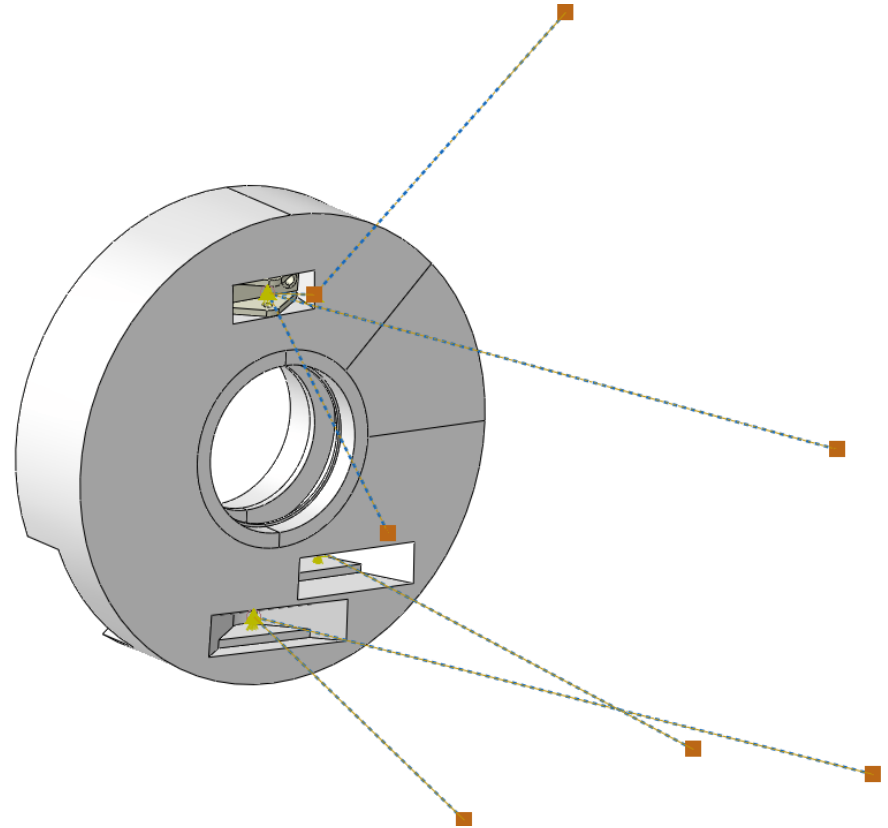
- Suspension arms
- Brakes
- Electrical motor



# The Workflow

## 1. Design domain

2. Properties
3. Mesh
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation



# The Workflow

1. Design domain
2. Properties
  - **Ti6Al4V**
  - **Density**
  - **Elastic Modulus**
3. Mesh
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation

## Material data sheet

### Mechanical properties of parts

	As built	Heat treated [6]
<b>Tensile strength [5]</b>		
- in horizontal direction (XY)	typ. 1230 ± 50 MPa typ. 178 ± 7 ksi	min. 930 MPa (134.8 ksi) typ. 1050 ± 20 MPa (152 ± 3 ksi)
- in vertical direction (Z)	typ. 1200 ± 50 MPa typ. 174 ± 7 ksi	min. 930 MPa (134.8 ksi) typ. 1060 ± 20 MPa (154 ± 3 ksi)
<b>Yield strength (R<sub>0.2</sub>) [5]</b>		
- in horizontal direction (XY)	typ. 1060 ± 50 MPa typ. 154 ± 7 ksi	min. 860 MPa (124.7 ksi) typ. 1000 ± 20 MPa (145 ± 3 ksi)
- in vertical direction (Z)	typ. 1070 ± 50 MPa typ. 155 ± 7 ksi	min. 860 MPa (124.7 ksi) typ. 1000 ± 20 MPa (145 ± 3 ksi)
<b>Elongation at break [5]</b>		
- in horizontal direction (XY)	typ. (10 ± 2) %	min. 10 % typ. (14 ± 1) %
- in vertical direction (Z)	typ. (11 ± 3) %	min. 10 % typ. (15 ± 1) %
<b>Modulus of elasticity [5]</b>		
- in horizontal direction (XY)	typ. 110 ± 10 GPa typ. 16 ± 1.5 Msi	typ. 116 ± 10 GPa typ. 17 ± 1.5 Msi
- in vertical direction (Z)	typ. 110 ± 10 GPa typ. 16 ± 1.5 Msi	typ. 114 ± 10 GPa typ. 17 ± 1.5 Msi
<b>Hardness [7]</b>		
	typ. 320 ± 12 HV5	

[5] Tensile testing according to ISO 6892-1:2009 (B) Annex D, proportional test pieces, diameter of the neck area 5 mm (0.2 inch), original gauge length 25 mm (1 inch).

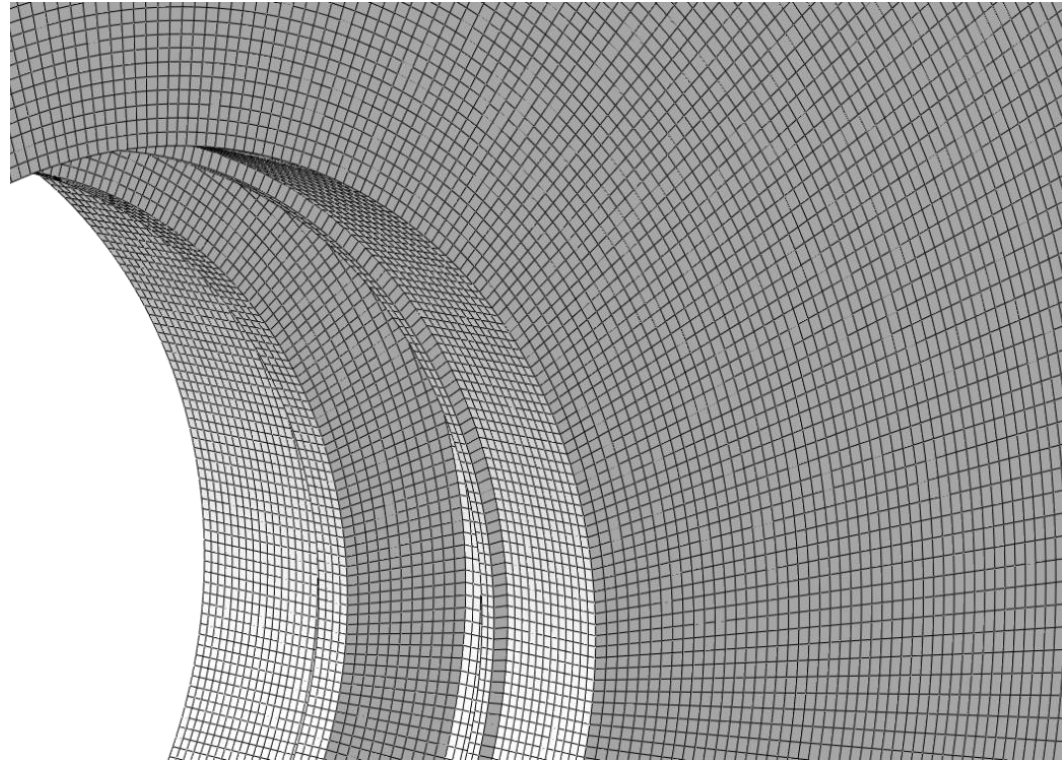
[6] Specimens were treated at 800 °C (1470 °F) for 4 hours in argon inert atmosphere. Mechanical properties are expressed as minimum values to indicate that mechanical properties exceed the minimum requirements of material specification standards. ASTM F1472-08. By fulfilling these minimum values, also the specifications of standards ASTM B348-09 and ISO 5832-3:2000 are met.

[7] Vickers hardness measurement (HV) according to EN ISO 6507-1 on polished surface. Note that measured hardness can vary significantly depending on how the specimen has been prepared.



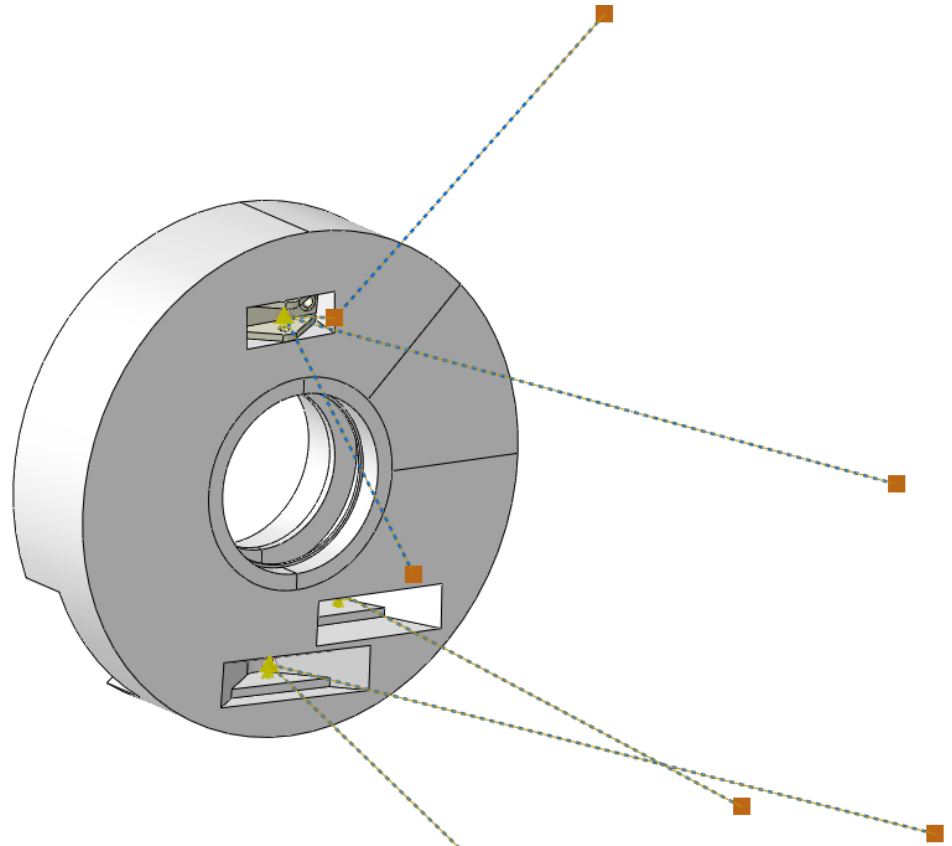
# The Workflow

1. Design domain
2. Properties
3. Mesh
  - **Structured Hexahedral elements**
  - **1 070 000 elements**
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation



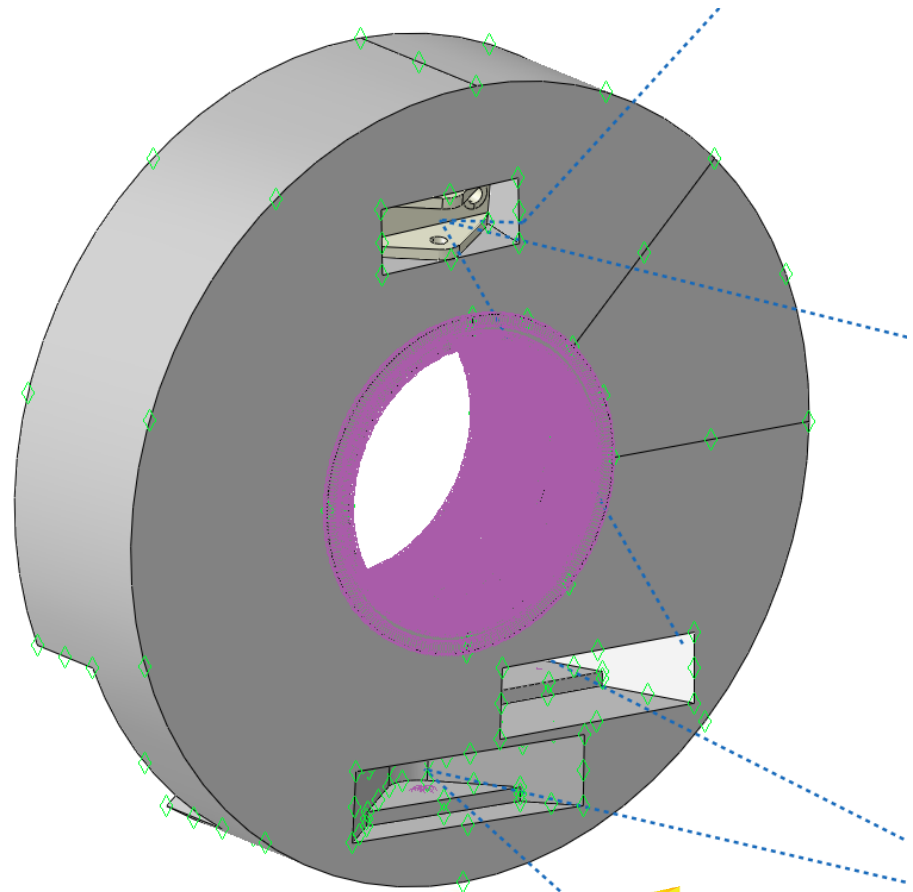
# The Workflow

1. Design domain
2. Properties
3. Mesh
4. Interactions
  - **Suspension points**
  - **Mounting bracket**
  - **Brake caliper**
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation



# The Workflow

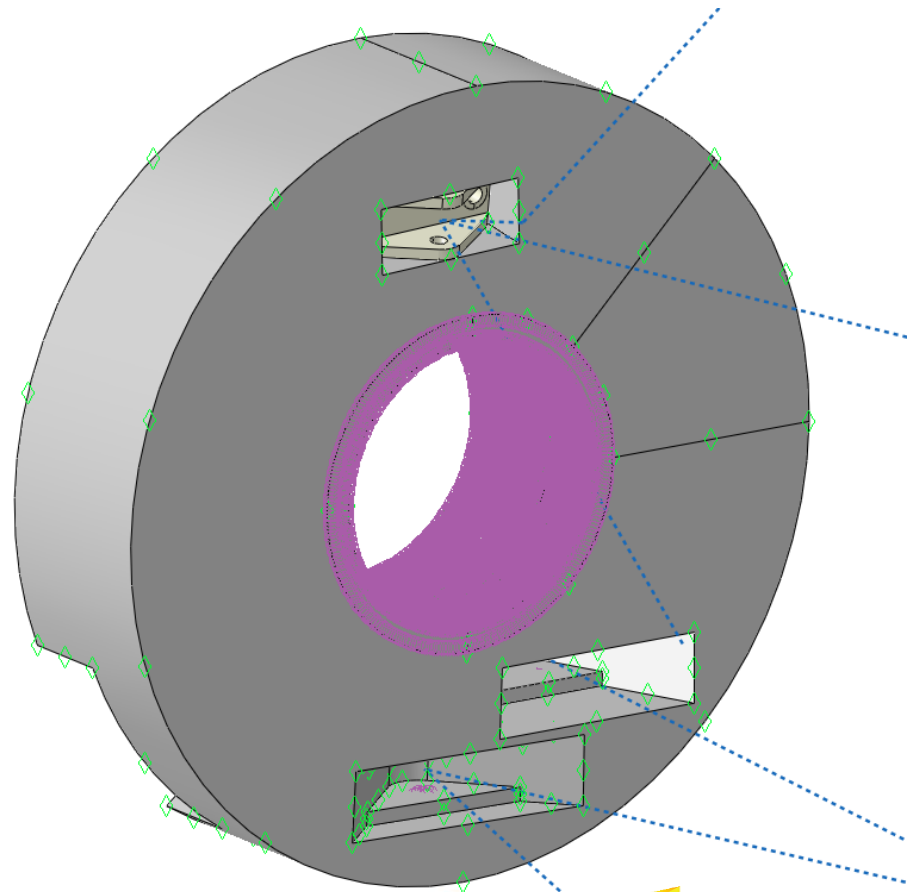
1. Design domain
2. Properties
3. Mesh
4. Interactions
- 5. Loads and boundary conditions**
  - **Wheel bearing reaction forces**
  - **Mapped analytical fields**
  - **Four quasi-static scenarios**
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation



VINU Jørgen Eliassen  
NTNU 2017

# The Workflow

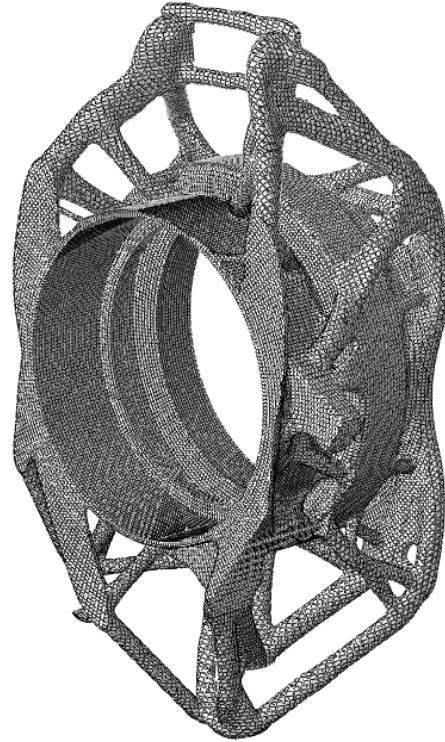
1. Design domain
2. Properties
3. Mesh
4. Interactions
5. Loads and boundary conditions
- 6. Optimization setup**
  - **Sensitivity-based algorithm**
  - **Minimum Compliance problem**
  - **Weight target**
7. Pre-processing
8. CAD regeneration
9. FE Validation
10. AM support generation



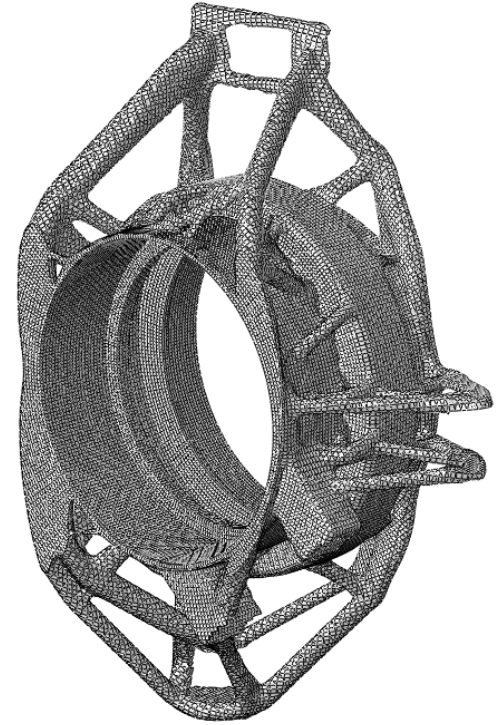
VINU Jørgen Eliassen  
NTNU 2017

# The Workflow

1. Design domain
2. Properties
3. Mesh
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
- 7. Pre-processing**
  - **Filtering**
  - **Smoothing**
8. CAD regeneration
9. FE Validation
10. AM support generation



Front



Rear

# The Workflow

1. Design domain
2. Properties
3. Mesh
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
- 8. CAD regeneration**
  - **Modifications for mounting holes**
  - **Inclusion of additional details (motor mount, seal slots,...)**
9. FE Validation
10. AM support generation

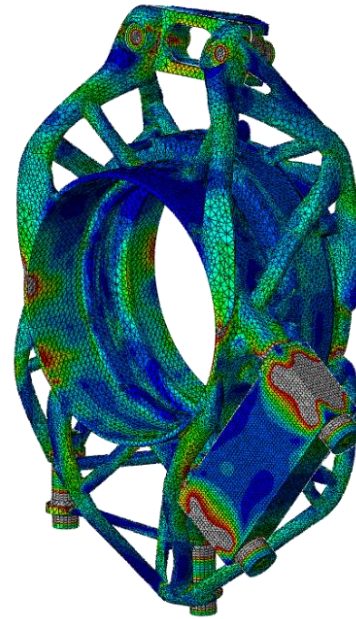
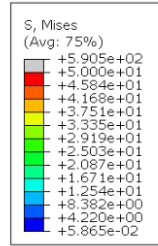


Front

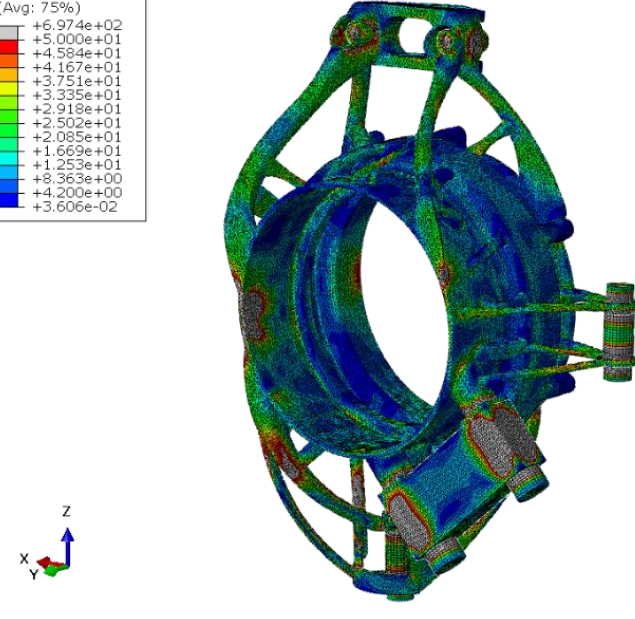
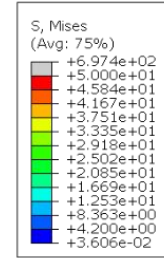
Rear

# The Workflow

1. Design domain
2. Properties
3. Mesh
4. Interactions
5. Loads and boundary conditions
6. Optimization setup
7. Pre-processing
8. CAD regeneration
9. FE Validation
  - Dimensioning load scenario
  - Extreme load scenario
  - Non-linearities (contact, pretension)
10. AM support generation

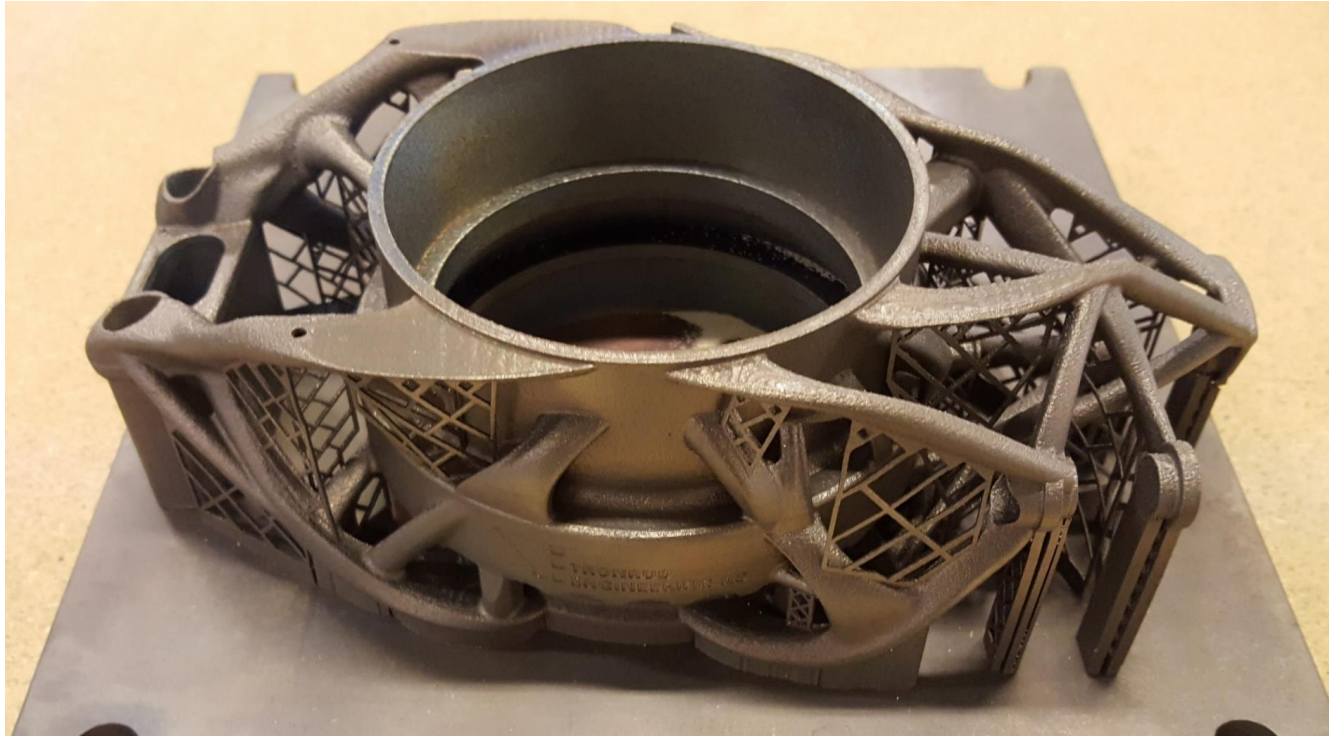


Front



Rear

# The Workflow





# The Workflow



Front upright post CNC-machining



Rear upright post CNC-machining

# The Workflow



# Compliance Model- An example

Dynamic wheel loads  
Tire-track interaction  
Weight transfer

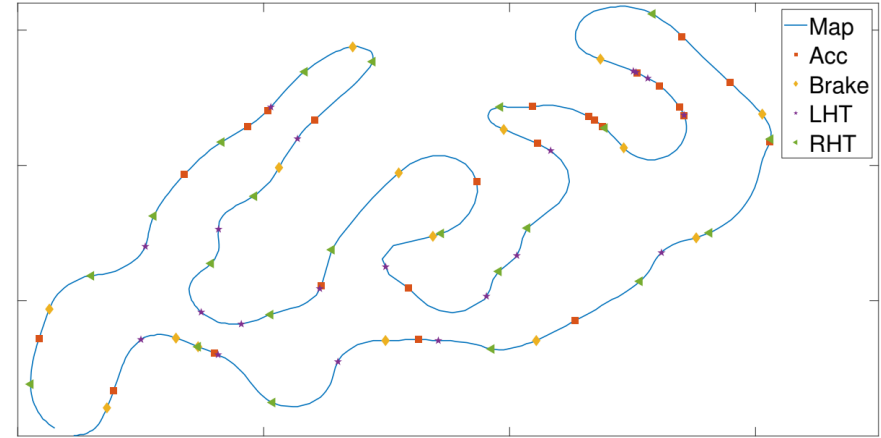


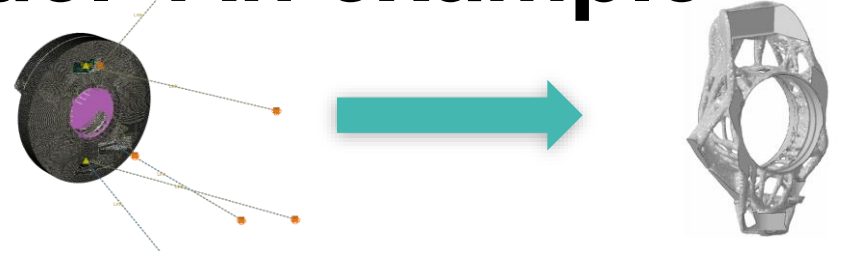
Figure 3.1: Load scenarios during FSG, longitude and latitude data from INS plotted. The car drives in the clockwise direction. Acc = Acceleration, LHT = Left Hand Turn, RHT = Right Hand Turn

# Compliance Model- An example

Material: EOS Ti6Al4V/ EOS Al10MgSi

Discretization

- Element type: Structured hexahedral
- Mesh method: Top-down combined with bottom-up



Loads: From tire tests – wheel bearing reaction forces used in optimization is calculated in collaboration with SKF

Upright	Iterations	Total iteration time [h]	TO raw weight [g]	Weight after regeneration [g]
Front left	72	95.2	374.6	577.9
Rear left	56	59.4	323.6	532.7
Rear right	49	46.3	324.2	524.5

Abaqus load definition: 4 independent quasi-static load scenarios defined with linear perturbation steps

Design responses: Strain energy (all steps)  
Weight

Objective function: Minimum compliance

Constraint: Weight target 350g

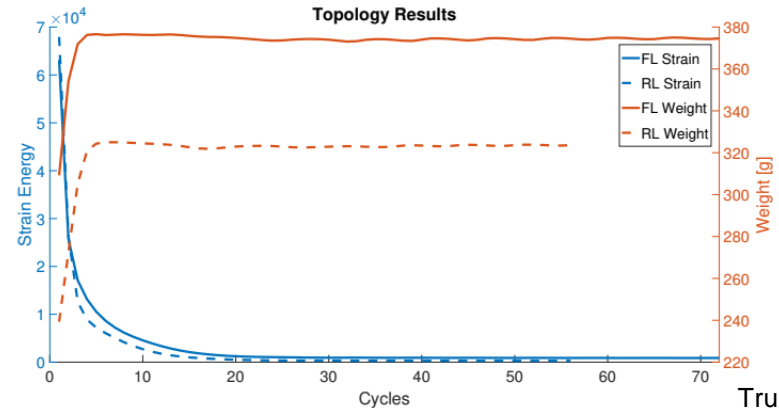


Figure 4.1: Results from Tosca Structure for front left and rear right upright

Truls Skoglund  
NTNU 2019

# Compliance Model- Material Selection

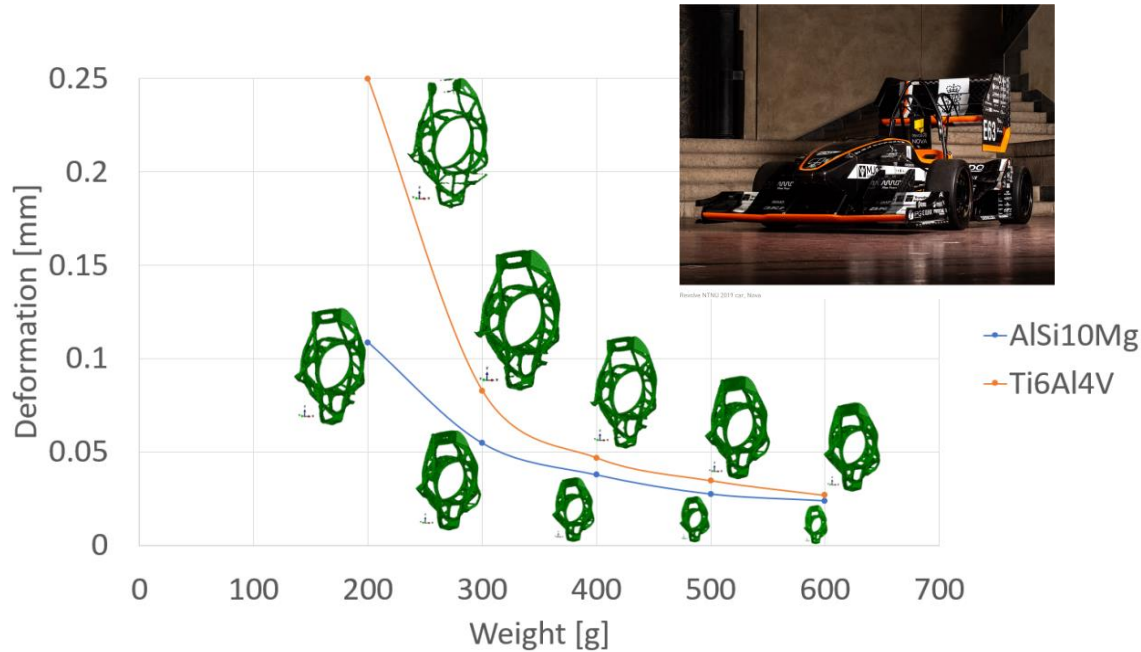


Figure 2.6: Comparison between upright in AlSi10Mg and Ti6Al4V, Skoglund (2019)

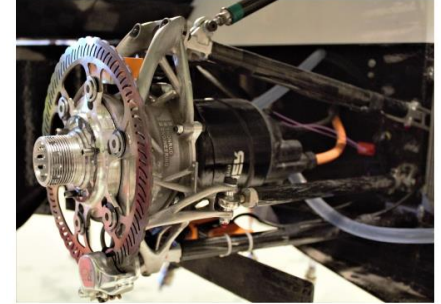


Figure 4.11: Rear left upright



Figure 4.12: Rear right upright

# What is performance?- the objective

Efficiency

Flow resistance

Material used

Stiffness/ Weight

Corrosion resistance

Dissassembly

Conductance

Manufacturing complexity

Surface area

Power

Eigenfrequency

Number of parts

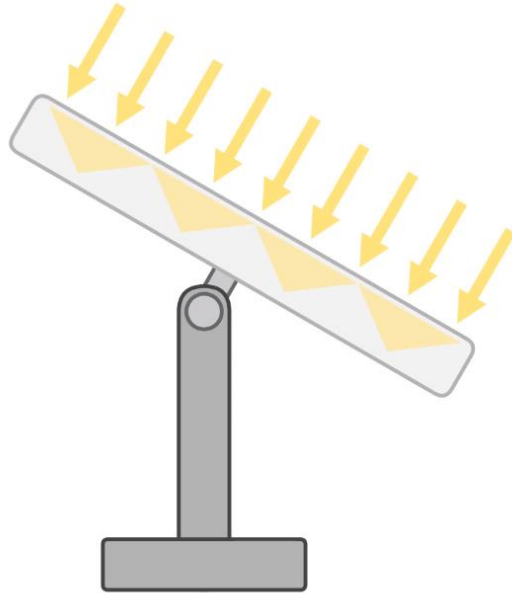
Transmittance

Accessibility

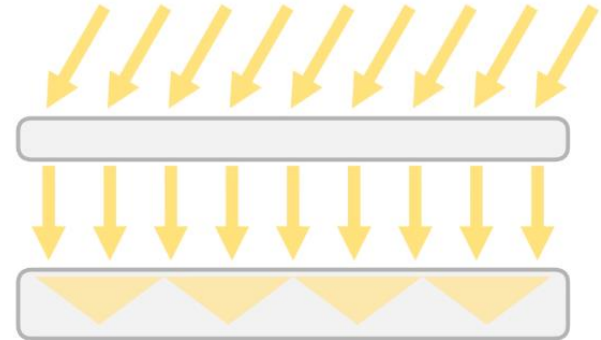
Cost

# Beyond stiffness- Solar Concentrator

Common tracker



Tracking integration with beam steering lens array



- No Rotation
- Low Physical Footprint
- Low Power, Fast, Accurate Tracking

# Solar concentration with BSLAs

Objective Function  
Boundary Conditions

- (1) Maximize efficiency in redirecting sunlight  $\uparrow \eta$

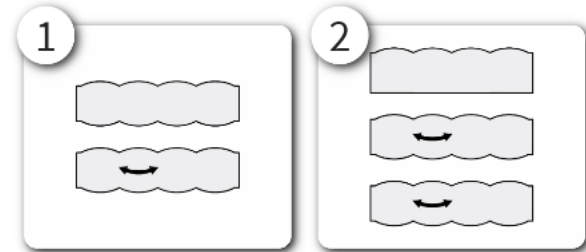
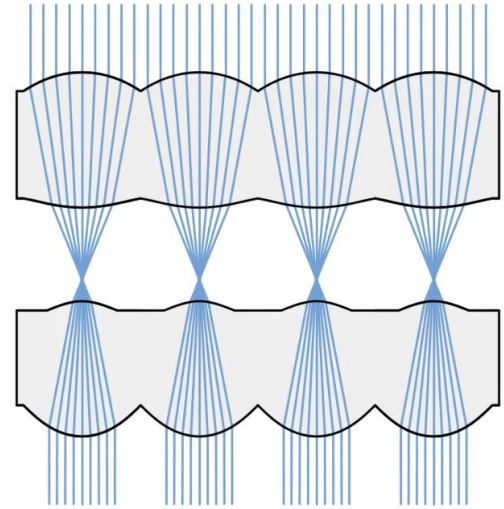
**Ingoing/ Outgoing intensity**

- (2) At a set divergence angle  $\downarrow \Theta_{\max}$

**Deviation of outgoing rays from surface normal**

- (3) At a set cost/complexity of the system  $\downarrow \$$

**# Parts/ Complexity of movement**

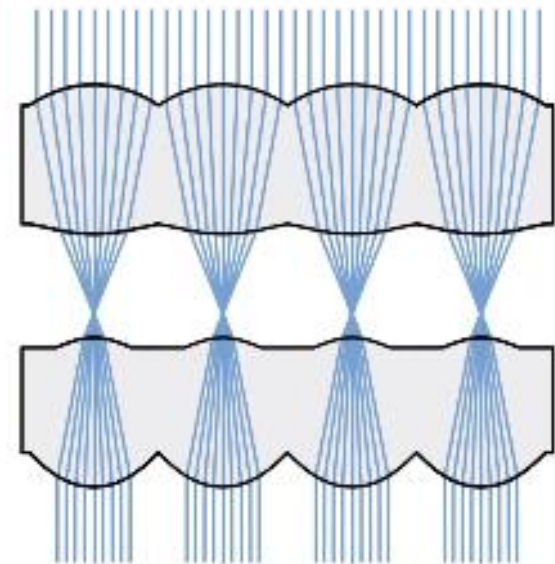
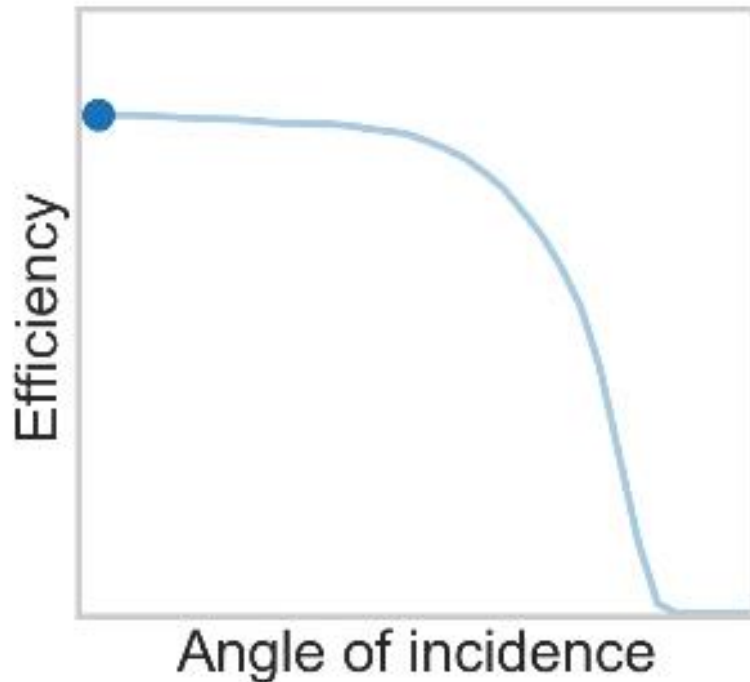


Johnsen et al. - Optics Express 2020



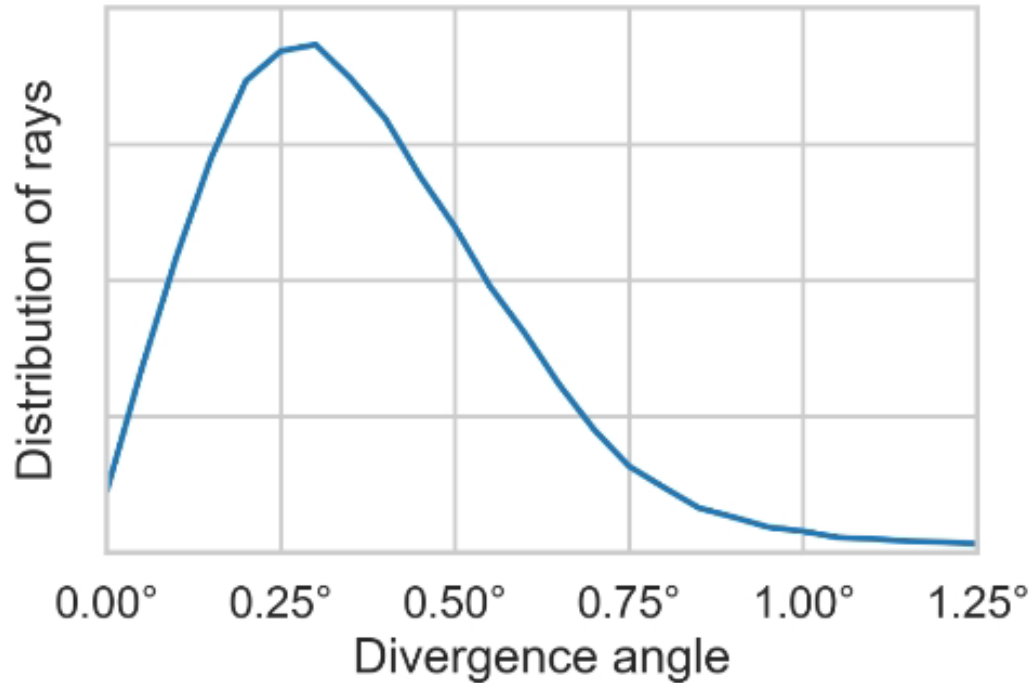
# Solar concentration with BSLAs

Maximize efficiency in redirecting sunlight  $\uparrow \eta$



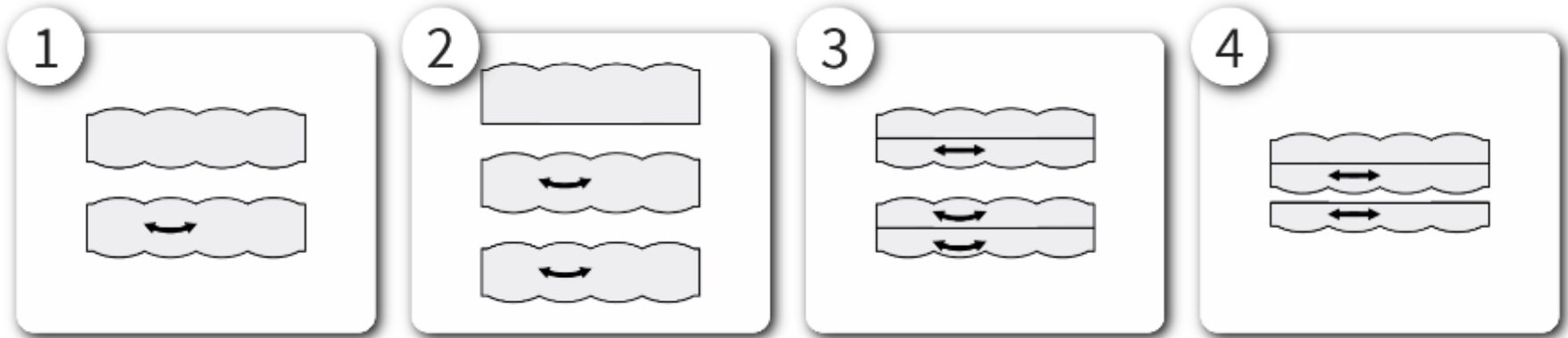
# Solar concentration with BSLAs

Minimize divergence of ingoing sunlight  $\downarrow \Theta_{\max}$



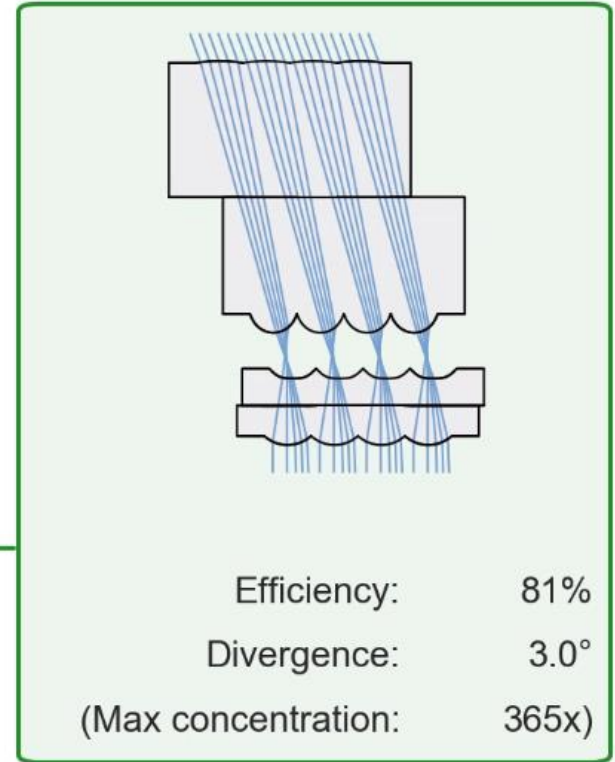
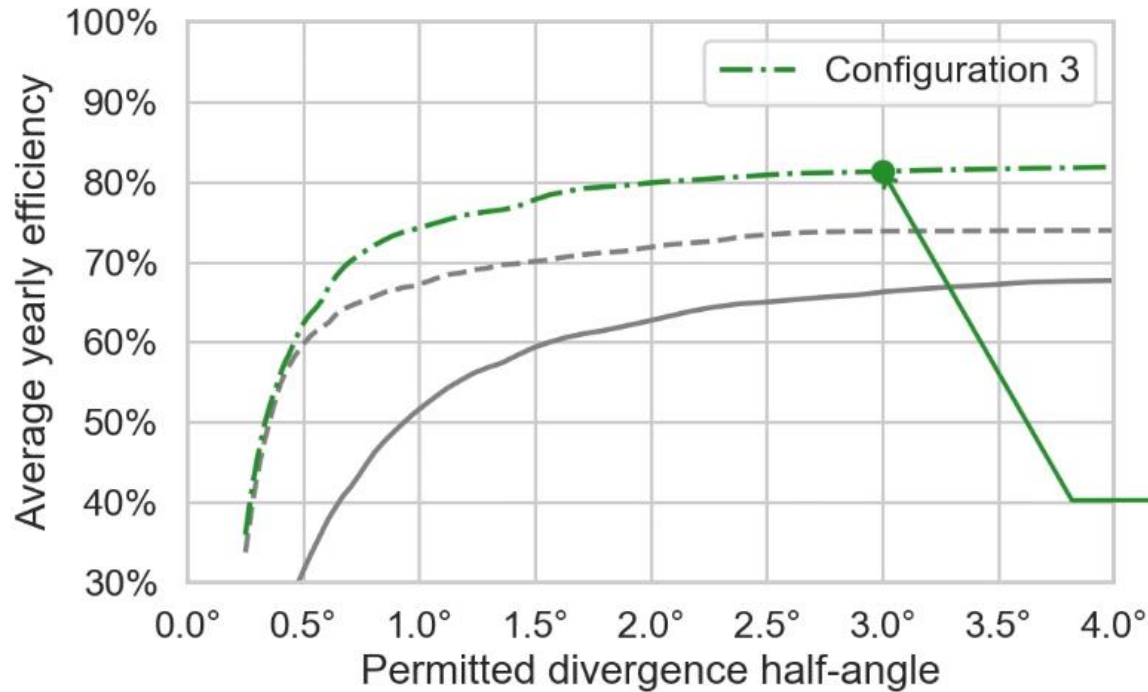
# Solar concentration with BSLAs

Minimize the cost/complexity of the system ↓\$

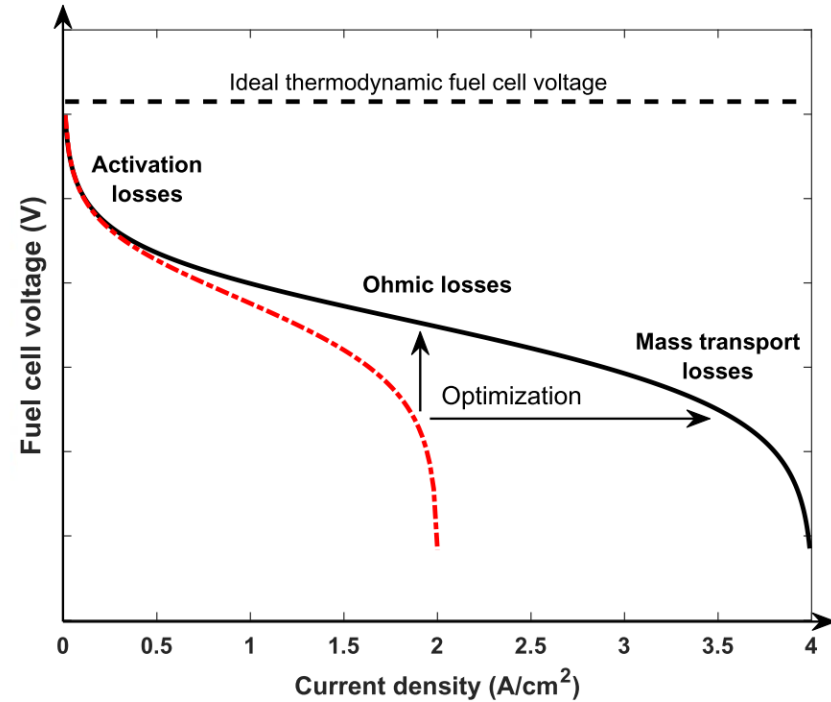
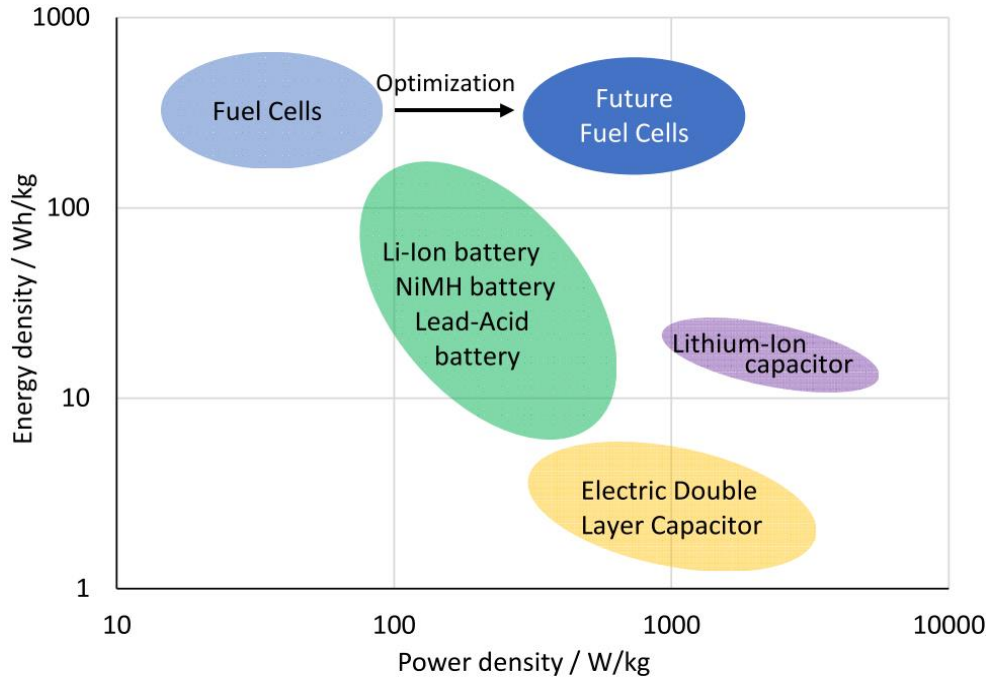


- Number of lens arrays
- Number of moving parts
- Number of sliding interfaces

# Solar concentration with BSLAs



# Next generation PEMFCs



O'Hare et al. – Wiley 2016

# The Gas Diffusion Layers

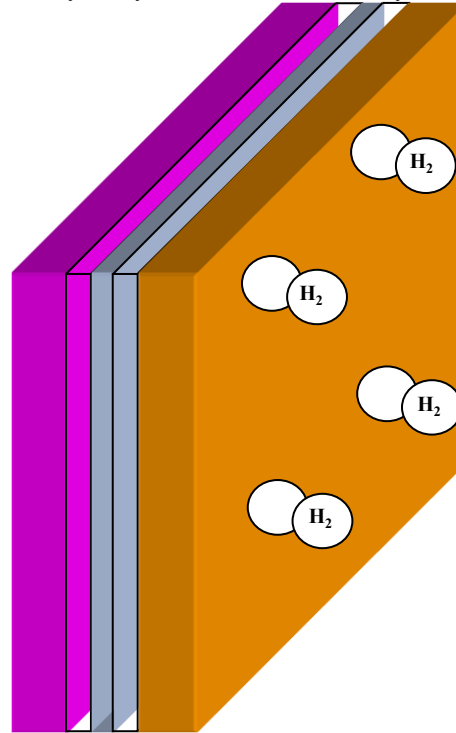
Oxidant

Gas Diffusion / Catalyst Layer

Electrolyte

Gas Diffusion / Catalyst Layer

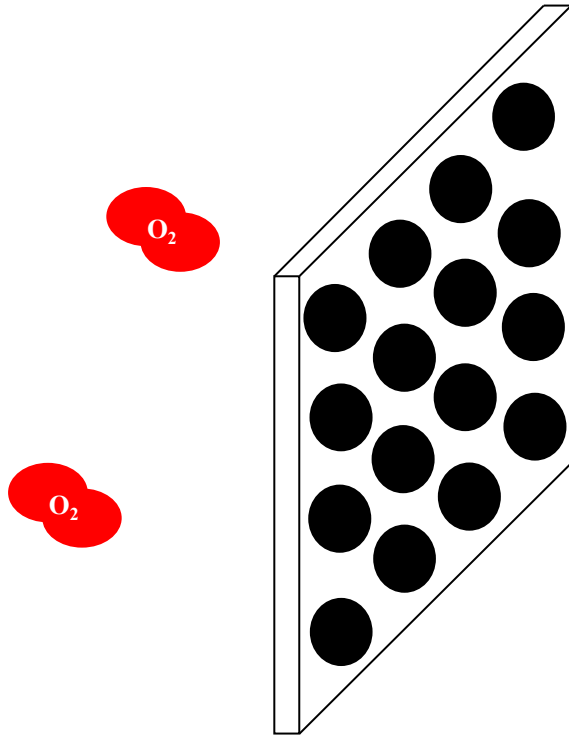
Fuel



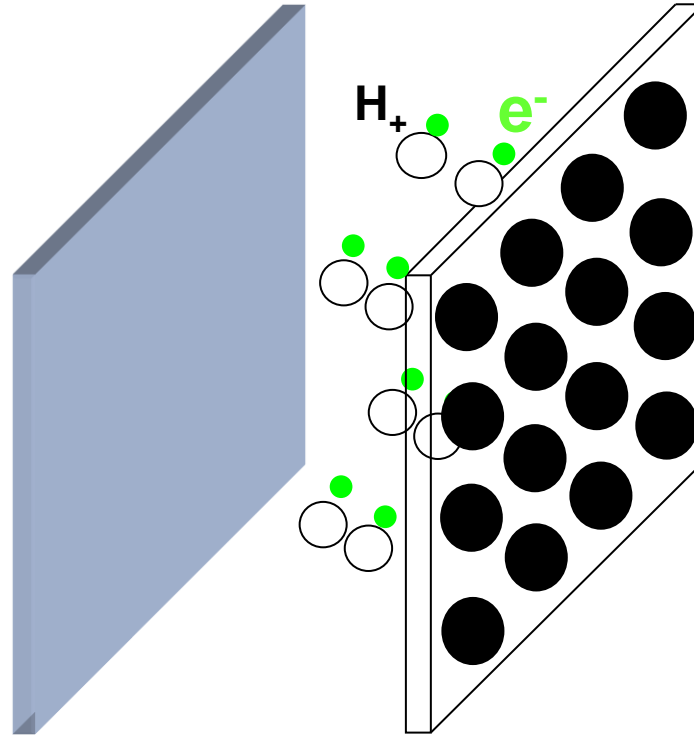
Cathode

Anode

Adapted from Prinz- ME260 Lecture Slides

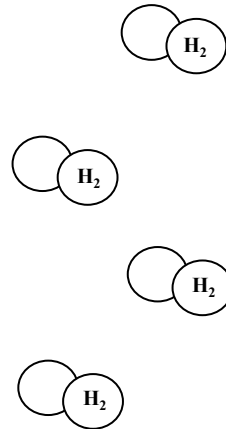


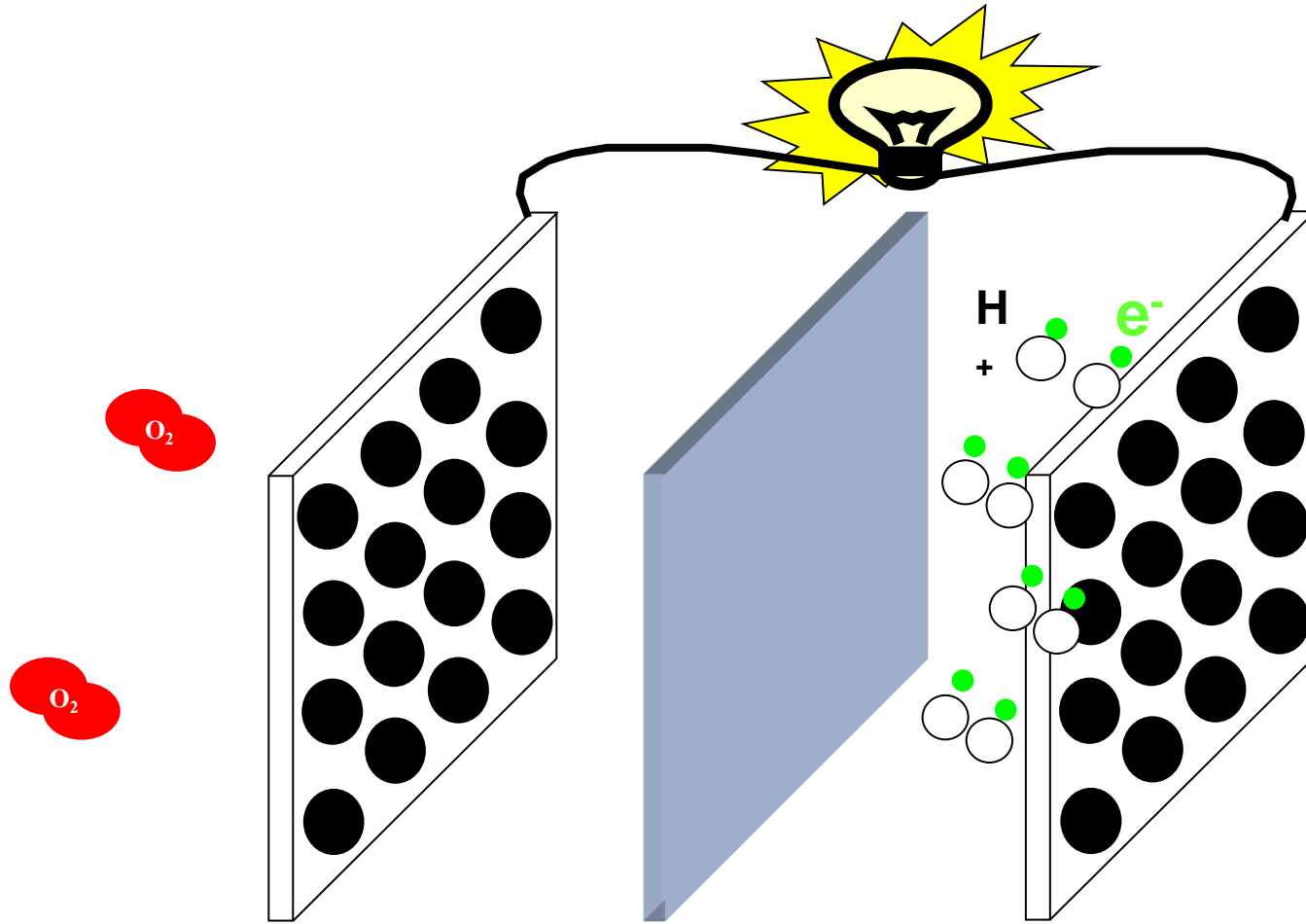
Cathode



Anode

Adapted from Prinz- ME260 Lecture Slides



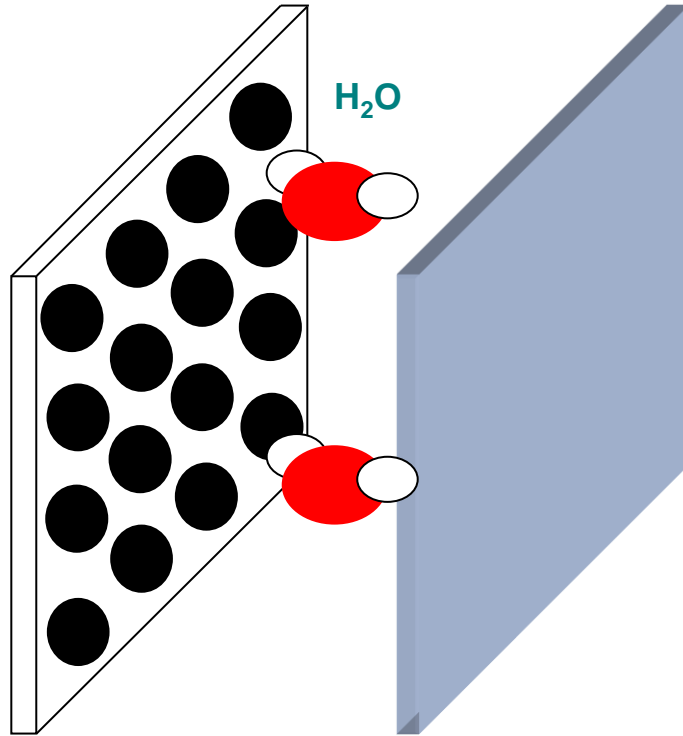


Cathode

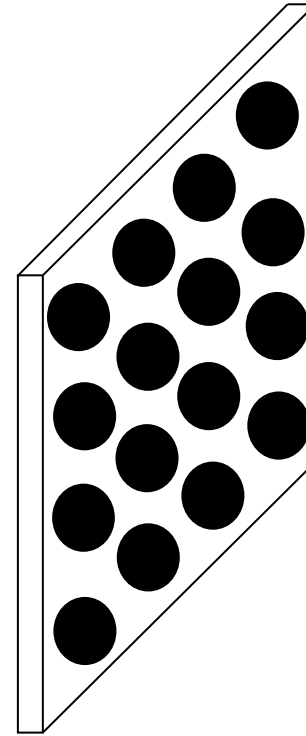
Anode

Adapted from Prinz- ME260 Lecture Slides





Cathode



Anode

Adapted from Prinz- ME260 Lecture Slides

# The optimum Gas Diffusion Layer

Objective Function  
Boundary Conditions

- (1) Maximize fuel cell power density  $\uparrow p$

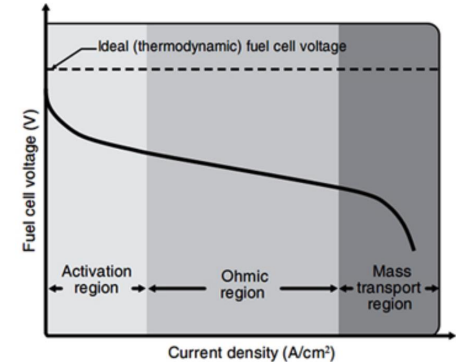
**Determined by activation losses, ohmic losses and transport losses**

- (2) At a given current density reange  $i_{\text{curr.1}}$

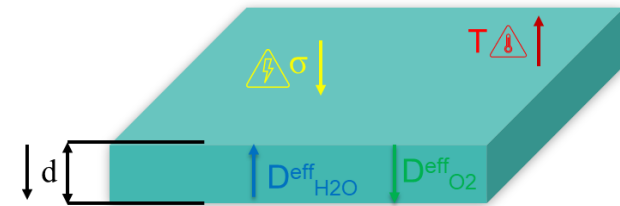
**Defines the dominating losses**

- (3) At given design constraints  $\downarrow d, \uparrow T, \uparrow \sigma, \uparrow D_{\text{H}_2\text{O}}^{\text{eff}}, \uparrow D_{\text{air}}^{\text{eff}}$

**The ranges of the design variables are interrelated**

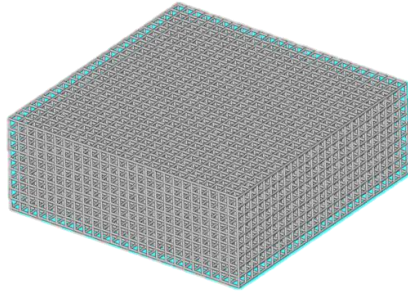


O'Hayre et. al.- Wiley 2016



Torgersen and Bock- ECS Prime 2020

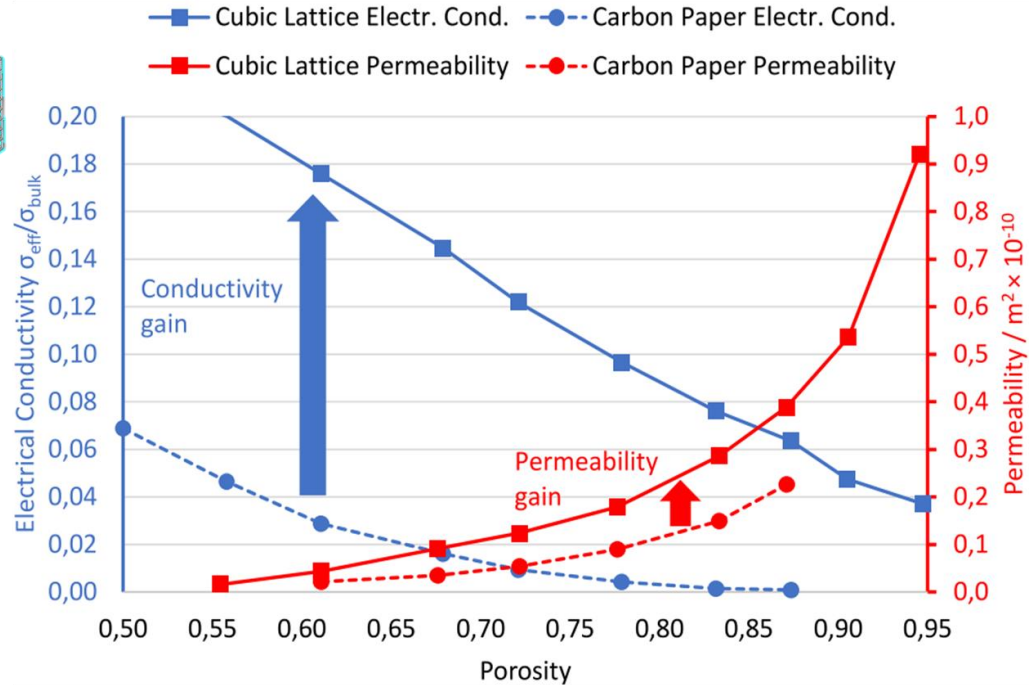
# The optimum Gas Diffusion Layer



Cubic Lattice

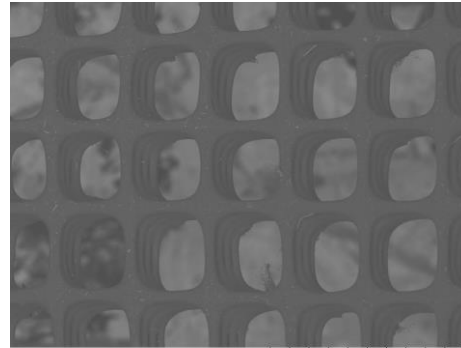


Carbon Paper



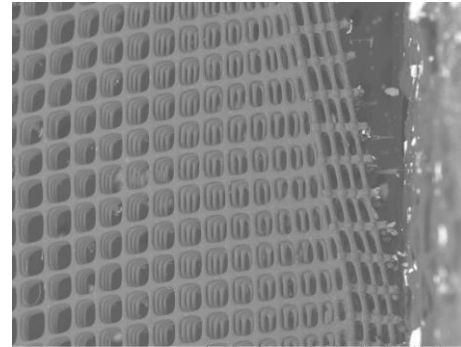
Data from Niblett et al.- Electrochem Soc 2020

# The optimum Gas Diffusion Layer



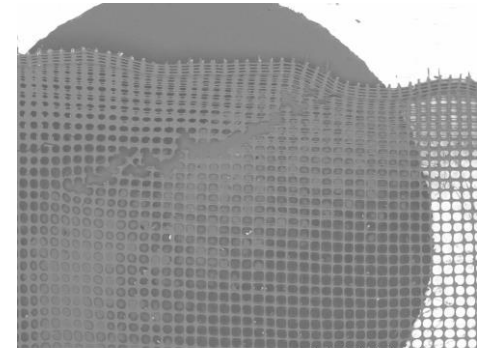
2020.10.05 13:32 F D8,3 x250 300 um

Compo



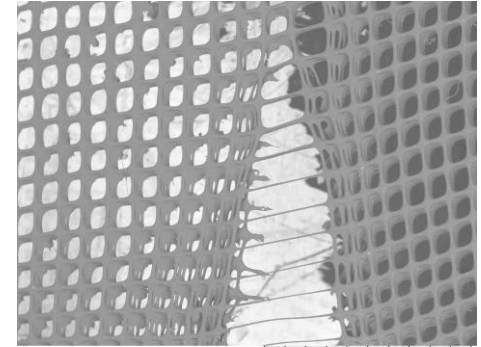
2020.10.05 14:06 F D7,2 x100 1 mm

Compo



2020.10.05 13:52 F D9,7 x30 2 mm

Compo



2020.10.05 13:56 F D8,3 x80 1 mm

Compo

# Design to...

Additive Production

Topology Optimization

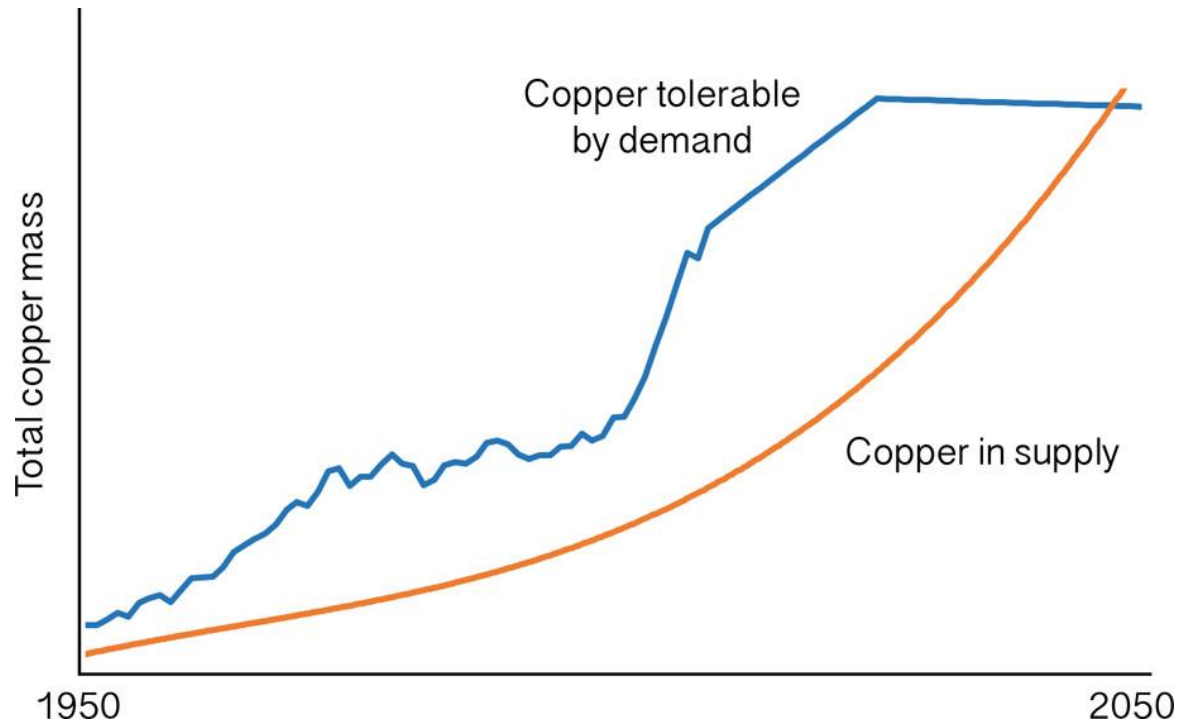


Save Material

Gain performance

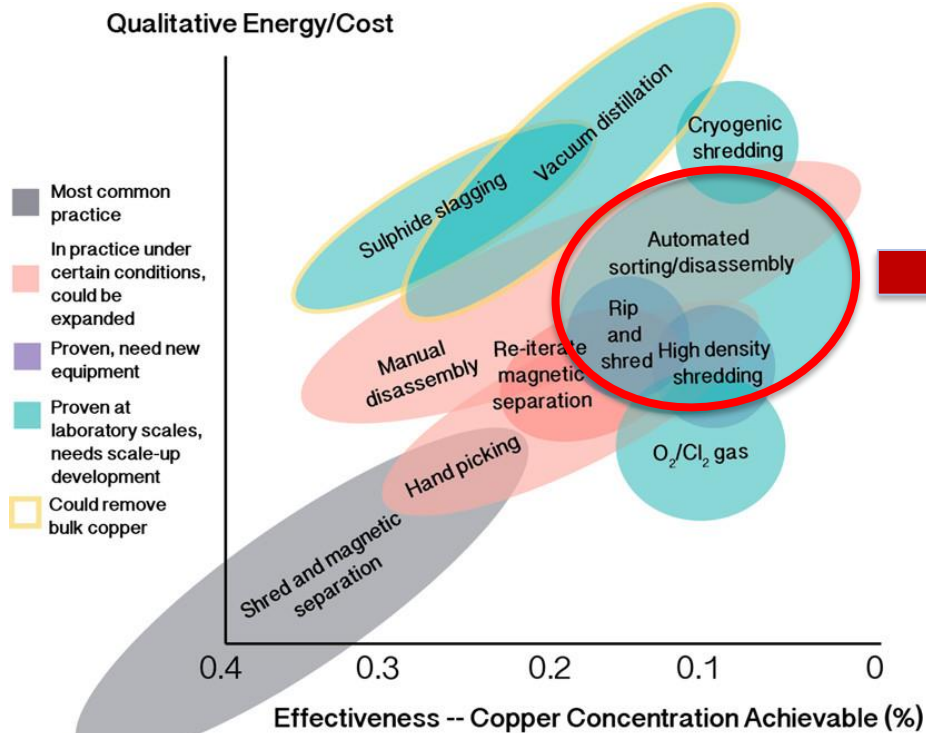
Reuse

# Design for Dissassembly



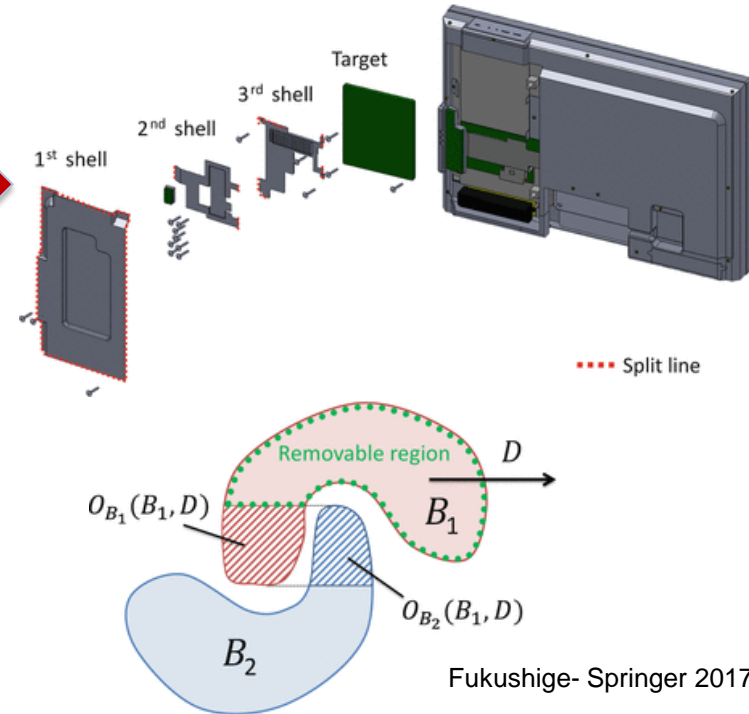
# Design for Dissassembly

Qualitative Energy/Cost



Daehn et al.- Envir. Sci. and Techn. 2017

Disassembly embedded design



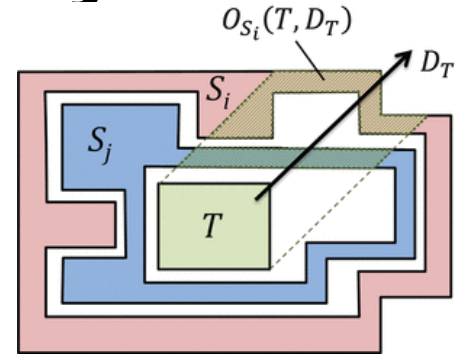
Fukushige- Springer 2017

# Design for Dissassembly

Objective Function

- (1) Minimize obstacle region  $\downarrow O_{S_i}$  by changing extraction direction  $D_i$

**Determined by size of Target component T**



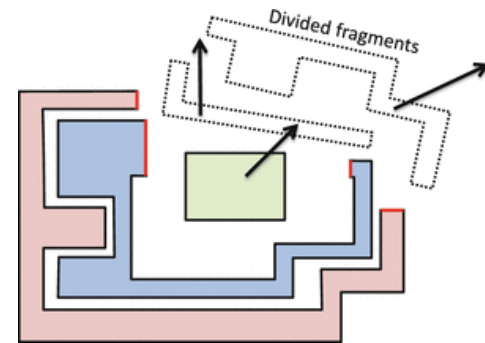
Boundary Conditions

- (2) At a given number of shells  $S_i$

**Given by the design**

- (3) At allowed number of split lines

**Sets the amount of disassembly operations**





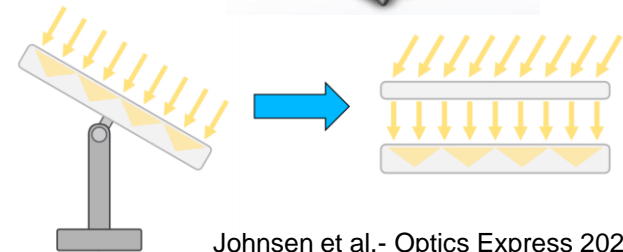
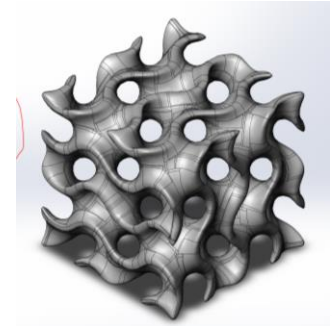
# Conclusion

- Additive Manufacturing offers new solutions
- Topology Optimization can infuse Innovation in Product Design
- Million design iterations at low cost
- Readily available: Lightweight and stiff organic designs
- Future possibilities: solar trackers, next generation fuel cells, material recycling

Interested?  
[Jan.torgersen@ntnu.no](mailto:Jan.torgersen@ntnu.no)



NTNU 2017



Johnsen et al. - Optics Express 2020